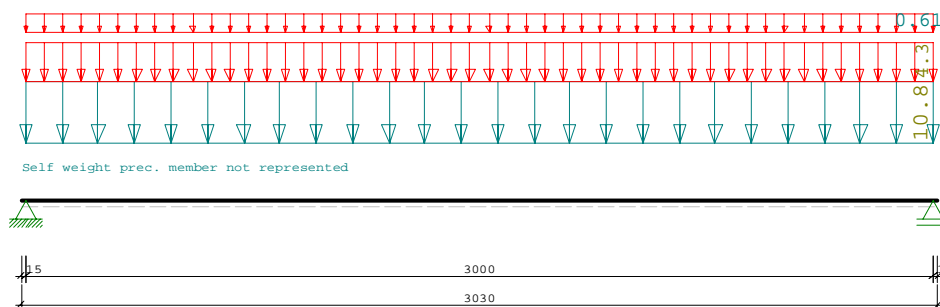
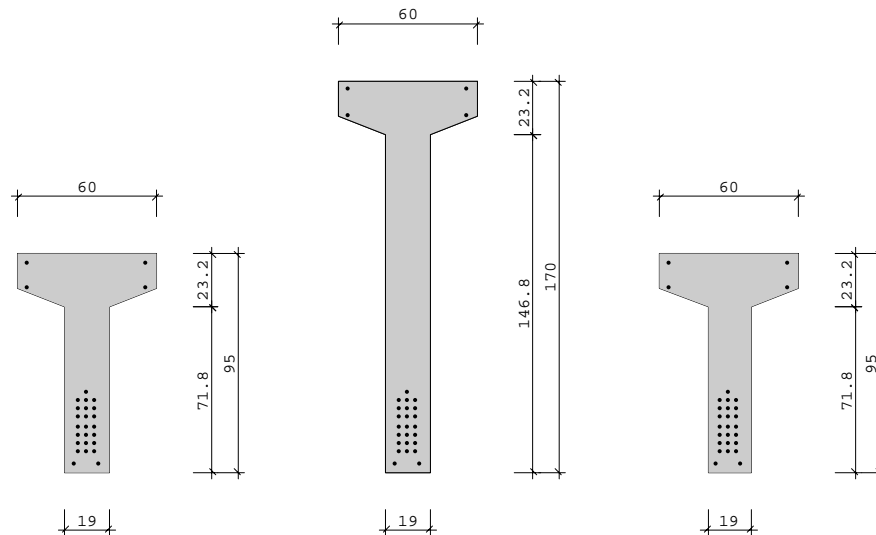
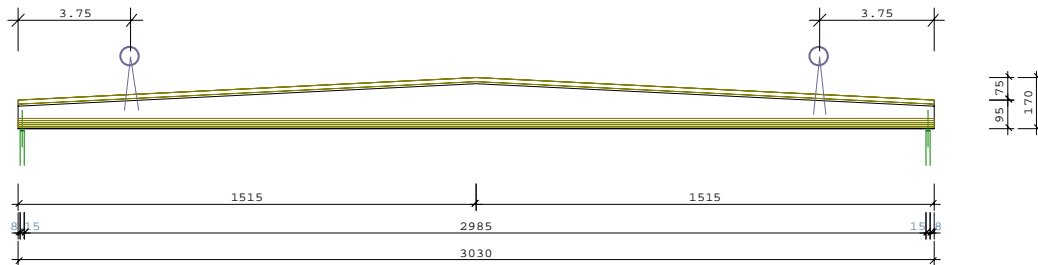




B8_001_FDB-Reference_eng Calculation example

Prestressed Concrete Girder B8 02/2022 (FRILO alpha)



System:

Double-pitch roof

Basics:

Load combinatorics: NA to BS EN 1990/A1:2009-06 + EN 1990:2002/AC:2010
 ULS: Structural safety checks(STR)
 permanent/variable design situation with equation 6.10 a,b



Design code: NA to BS EN 1992-1-1/A2:2015-07 + EN 1992-1-1:2004 /AC:2010
Prestressing for pretensioning with heat treatment in stressing mould

System Geometry:

Total L = 30.30 m Effective L1 = 30.00 m
Outstand left L0 = 0.15 m right L2 = 0.15 m
Distance Ridge L3 = 15.15 m
Height beam :
left H1 = 95.0 cm Ridge H2 = 170.0 cm
right H3 = 95.0 cm
Relation eff.span to height of beam:
L1/H2 = 17.65

Erection attachment, distance from the beginning resp. end of beam:
Hook L8 = 3.75 m right L9 = 3.75 m

Cross-section Precast :

Layer of cross-section from top to bottom			
Nr	Width [cm]	Distance [cm]	Remarks
1	60.0	0.0	
2	60.0	15.0	
3	19.0	23.2	Web begin
4	19.0	170.0	Web end
Top flange height over beam length constant			

Material:

Prestressing steel

Y1770S7 Strand 7 wires

$d_d = 4.1$ mm $d_p = 12.3$ mm
 $E_p = 195000$ N/mm² $A_p = 0.930$ cm²
 $f_{p0.1k} = 1520$ N/mm² $f_{pk} = 1770$ N/mm²
 $\epsilon_{uk} = 35.0$ ‰ $\epsilon_{ud} = 31.5$ ‰

Partial safety factor :

$\gamma_s = 1.15$

Coeff. prestress:

charact. value $r_{sup} = 1.00$ $r_{inf} = 1.00$
Design value $\gamma_{p,max} = 1.10$ $\gamma_{p,min} = 0.90$

Proof of crack width

Equ. diameter $d_{pv} = 7.20$ mm $\xi = 0.60$ (Tab. 6.2)

Relaxation class 2 (strands, wires, low relaxation)				
σ_{p0}/f_{pk}	10 h	200 h	1000 h	500000h
0.60	0.1	0.2	0.4	2.5
0.70	0.3	0.7	1.0	3.9
0.80	1.2	1.9	2.4	6.1
- Losses in % by 3.3.2 (6), example process				

Permitted stresses:

in formwork $\sigma_p \leq 1368.0$ N/mm² ($0.90 \cdot f_{p0.1k}$)
after anchor. release $\sigma_p \leq 1292.0$ N/mm² ($0.85 \cdot f_{p0.1k}$)
char. Lc $\sigma_p \leq 1327.5$ N/mm² ($0.75 \cdot f_{p0.1k}$)



Transmission length

$$\begin{aligned} \eta_{p1} &= 3.20 & \eta_1 &= 1.00 \\ \alpha_1 &= 1.25 & \alpha_2 &= 0.19 \\ \sigma_{pm0} &= 882 \text{ N/mm}^2 \\ \text{PT: } f_{ctdt} &= 0.81 \text{ N/mm}^2 & f_{bpt} &= 2.58 \text{ N/mm}^2 \\ l_{pt} &= 1.00 \text{ m} \end{aligned}$$

Dispersion_length:

$$d = 0.91 \text{ m} \quad l_{disp} = 1.35 \text{ m}$$

Reinforcing steel:

Longitudinal B 500B		Stirrup B 500B	
$E_s =$	200000 N/mm ²	$E_s =$	200000 N/mm ²
$f_{yk} =$	500 N/mm ²	$f_{yk} =$	500 N/mm ²
$f_{tk} =$	540 N/mm ²	$f_{tk} =$	540 N/mm ²
$\epsilon_{uk} =$	50.0 ‰	$\epsilon_{uk} =$	50.0 ‰
$\epsilon_{ud} =$	45.0 ‰	$\epsilon_{ud} =$	45.0 ‰

Partial safety factor :

$$\gamma_s = 1.15 \quad \gamma_s = 1.15$$

permitted stresses in SLS :

$$\sigma_s \leq 400 \text{ N/mm}^2 \quad \sigma_s \leq 400 \text{ N/mm}^2 \quad (0.80 * f_{yk})$$

Requirements durability:

	top	bottom
attack on concrete	X0	X0
attack on reinforc.	XC1	XC1
min. concrete class	C 20/25	C 20/25
stirrup	$\phi_l = 8 \text{ mm}$	
long. reinforcement	$\phi_m = 20 \text{ mm}$	$\phi_m = 16 \text{ mm}$
prestressed steel	$d_p = 12.3 \text{ mm}$ strand	
allowance in design	$\Delta c_{dev} = 5 \text{ mm} *2$	$\Delta c_{dev} = 5 \text{ mm} *2$
stirrup	$c_{min,l} = 15 \text{ mm}$	$c_{min,l} = 15 \text{ mm}$
concrete coverage	$c_{nom,l} = 20 \text{ mm}$	$c_{nom,l} = 20 \text{ mm}$
longitudinal bars	$c_{min,m} = 20 \text{ mm} *5$	$c_{min,m} = 16 \text{ mm} *5$
concrete coverage	$c_{nom,m} = 28 \text{ mm} *1$	$c_{nom,m} = 28 \text{ mm} *1$
prestressing steel :	$c_{min,p} = 19 \text{ mm} *5$	$c_{min,p} = 19 \text{ mm} *5$
concrete coverage	$c_{nom,p} = 28 \text{ mm} *1$	$c_{nom,p} = 28 \text{ mm} *1$
laying dist. link	$c_l = 20 \text{ mm}$	$c_l = 20 \text{ mm}$
all. crack width	$w_{max} = 0.20 \text{ mm}$	$w_{max} = 0.20 \text{ mm}$
decompression	not req.	not req.
*1:with $c_{min,l}$		
*2: Quality Control		
*5: bond decisive		

Concrete:

Precast

$$\begin{aligned} &\text{C 50/60} \\ f_{ck} &= 50.00 \text{ N/mm}^2 \\ \alpha_{cc} &= 0.85 \\ f_{ctk0.05} &= 2.85 \text{ N/mm}^2 \\ \alpha_{ct} &= 1.00 \\ \gamma &= 25.00 \text{ kN/m}^3 \quad \text{Unit} \\ E_{cm} &= 37000 \text{ N/mm}^2 \\ \alpha_E &= 1.00 \quad \text{Coeff. E-module} \\ G_{cm} &= 14800 \text{ N/mm}^2 \end{aligned}$$

Partial safety factor :

$$\gamma_c = 1.50$$



permitted stresses in SLS :

char. Lc $\sigma_c \geq -30.00 \text{ N/mm}^2$

q.perm.Lc $\sigma_c \geq -22.50 \text{ N/mm}^2$

Removal the anchor $t = t_0T(sto) = 5.1 \text{ d}$

$f_{cm(t)} = 44.43 \text{ N/mm}^2$

$f_{ck(t)} = 36.43 \text{ N/mm}^2$

linear creep $\sigma_c \geq -16.39 \text{ N/mm}^2 \text{ (k2=0.45)}$

maximum $\sigma_c \geq -25.50 \text{ N/mm}^2 \text{ (k6=0.70)}$

Creep modulus & shrinkage strain

with heat treatment in stressing mould

$Tt_0 = 60^\circ\text{C}$ (until releasing the anchor)

$t_{eq} = 4533 \text{ h}$ (equivalent time difference for relaxation)

$t_0T = 5.1 \text{ d}$ (according to temperature adjusted concrete age)

CementStrength class 42,5R/52,5

$\rho = 0.5$ (Aging coefficient)

Reference point for t_0 is the start of the concreting of the precast

Creep	t0 Days	RH %
Storage	1	70
Utilization precast	21	50

L.	Segment	Part- cross-section	t0	t	α	$t_{0,eff}$ B.9	β_{t0} B.5	β_H B.8	$\beta_{c(t,t_0)}$ B.7	φ_{RH} B.3	β_{fcm} B.4	$\varphi(t,t_0)$ B.1
1	Storage	PcC	1.0	21.0	1	10.2	0.59	475.4	0.38	1.24	2.21	0.62
2	Utilization precast	PcC	21.0	26000.0	1	10.2	0.59	463.7	0.61	1.47	2.21	1.17

L.	A [cm ²]	U [cm]	h0 [cm]	$\beta_{ds}(t_0,ts)$	$\beta_{ds}(t,ts)$ 3.10	β_{RH} B.12	$\epsilon_{cd,0}$ B.11	β_{as} 3.13	$\epsilon_{ca}/10e6$ 3.12	$\epsilon_{cs}(t,t_0)$ [‰]
1	4013.10	446.8	179.7	0.000	0.172	1.02	402.5	0.60	100.00	0.121
2	4013.10	446.8	179.7	0.172	0.996	1.36	536.0	1.00	100.00	0.430

Loads:

Self weight

Beam beginning $g_{11} = 6.47 \text{ kN/m}$

Ridge $g_{12} = 10.03 \text{ kN/m}$

Beam end $g_{13} = 6.47 \text{ kN/m}$

Total $G = 250.1 \text{ kN}$

Volume $V = 10.00 \text{ m}^3$

Surf. $A = 95.00 \text{ m}^2$

Units: Single load[kN] Single moment[kNm] line load[kN/m]												
span	type	gle	qle	Dist. a [m]	gri	qri	Length [m]	Fact	Act.	Sim.	Alt.	Pos.
1	1	10.80	4.30					1.00	10	0	0	
1	1	0.00	0.61					1.00	9	0	0	
Load types: 1 = uniformly distr., 2 = single load at a, 3 = single moment at a 4 = trapezoidal load from a, 5 = triangle load over L												

Actions:

Act.	γ_0	ψ_0	ψ_1	ψ_2	Dep.	Cat.	Description
9	1.50	0.50	0.20	0.00	0	W	Wind loads
10	1.50	0.50	0.20	0.00	0	S	Snow loads <1000m

Tendons:

Dist(LE) > 3.5 cm axis horizontal > 3.7 cm vertical > 3.7 cm



lay. No.	num-ber	area Ap [cm²]	Dist.LE Yp [cm]	Prestressing $\sigma_p^{(0)}$ [N/mm²]	Count	<--- Isolations ---> to x1 [m]	from x2 [m]	Type
1	3	2.79	8.5	1000	0			LE
2	3	2.79	12.3	1000	0			LE
3	3	2.79	16.1	1000	0			LE
4	3	2.79	19.9	1000	0			LE
5	3	2.79	23.7	1000	0			LE
6	3	2.79	27.5	1000	0			LE
7	3	2.79	31.3	1000	0			LE
8	1	0.93	35.1	1000	0			LE

x1 and x2 with respect to the left beginning from joint
 LE= parallel lower edge, UE= parallel upper edge
 The calculation of the losses due to creep, shrinkage and relaxation following the method from Abelein

Untensioned reinforcement:

Layer No.	num-ber	diam. $\Phi_{s,l}$ [mm]	area As [cm²]	Dist.LE Ys [cm]	effective range		Type
					from xA [m]	to xE [m]	
1	2	16	4.02	3.6	0.00	30.30	LE
2	2	20	6.28	166.2	0.00	30.30	UE
3	2	20	6.28	155.0	0.00	30.30	UE

xA and xE with respect to the left beginning from joint
 LE= parallel lower edge, UE= parallel upper edge

Surface reinforcement acc.to Tab. NA.J.41 (B0 < D0) :

Web (Z1/S3) AsS = 1.24 cm²/m (Uwks <= XC4) (per side)
 Top flange (Z3/S1) AsO = 0.00 cm²/m (Uwks <= XC4)

Settings for shear resistance check

Bearing width, distance bearing edge, effective height of the bearing line

left bAl = 0.15 m al = 0.07 m dAl = 0.92 m

right bAr = 0.15 m ar = 0.07 m dAR = 0.92 m

For shear reinforcement not decisive ranges over support A and B:

xaRe=0.99 m direct bearing (width of bearing/2 + eff. depth)

xbLi=0.99 m direct bearing (width of bearing/2 + eff. depth)

Check the limit deformation:

Total sagging $f \leq L/250$ Increase deflection $|df| \leq L/500$

Cantilever left $f \leq 0.1$ cm $|df| \leq 0.1$ cm

Span $f \leq 12.0$ cm $|df| \leq 6.0$ cm

Cantilever right $f \leq 0.1$ cm $|df| \leq 0.1$ cm

quasi- permanent combination and eff. char. prestress

Deflection due to shrinkage considered

Tension stiffening: Member rigidity, Characteristic combination

RESULTS (summary)

Reaction forces (t = infinitely):

Units: all [kN] G:perm., Q:variable, V: Sum					
			<-----char. value----->	<--ULS(PT)---->	
Support point	G	min Q	max Q	min V	max V
A (left)	287.01	0.00	73.65	287.01	462.02
B (right)	287.01	0.00	73.65	287.01	462.02

max. bending moment in erection state(char. value):

MF = = 2763.72 kNm at x = = 15.15 m



Checks are not complied with:

Checkvalue		Extrem		Utilisation	x [m]
Resisting tens force bot	$\eta =$	0.86		1.16	30.15
Crack MinAs+AsDuc bottom A	AsMin =	6.7	cm ²	1.66	15.15
Prc.:Compr.stress t0(sto)	$\sigma_c =$	-27.31	N/mm ²	1.07	3.75
Buckling installed state (Stiglat)	$\eta =$	1.69		1.19	

Warning

Prc.:lin. creep t0(Sto) $\sigma_c = -23.09$ N/mm² x= 0.80 m

$\sigma_c < 0.45 \cdot f_{ck}(t) = -16.39$ N/mm²

_disproportional creeping by increased creep modulus considered($f_k = 1.32$)

Required shear reinforcement:

Column A: asw = 5.00 cm²/m

Column B: asw = 5.00 cm²/m

Bursting reinforcement

left Laying length = 1.02 m

from x = 0.00 m

As = 5.3 cm²

right Laying length = 1.02 m

from x = 30.30 m

As = 5.3 cm²

Check of anchorage

left: Tensile force resistance in anchoring area Util = 1.16

additional reinforcement necessary

right: Tensile force resistance in anchoring area Util = 1.16

additional reinforcement necessary

Overview crit. sections

Selected basic grid: 10 Sections

Checkvalue		Extrem		Utilisation	x [m]	
Flexural capacity bottom	$\eta =$	1.17		0.86	19.53	
Flexural capacity top	$\eta =$	6.64		0.15	3.75	
Resisting tens force bot	$\eta =$	0.86		1.16	30.15	!
Resisting tens force top	$\eta =$	6.64		0.15	3.75	
Prc.:Compr.stress t0(sto)	$\sigma_c =$	-27.31	N/mm ²	1.07	3.75	!
Prc.:Compr.stress Cc	$\sigma_c =$	-22.83	N/mm ²	0.76	3.75	
Stress in prestress.steel	$\sigma_p, Cc =$	1068.4	N/mm ²	0.80	19.19	
Stress in rebars	$\sigma_s =$	142.7	N/mm ²	0.36	10.81	
Crack MinAs+AsDuc bottom A	AsMin =	6.7	cm ²	1.66	15.15	!
Crack MinAs+AsDuc top A	AsMin =	----	cm ²	----	----	
Crack width bottom	wk =	0	mm	0.40	11.15	
Crack width top	wk =	0	mm	0.76	3.75	
Sagging top	fo =	-2.5	cm	0.20	13.47	
Sagging bottom	fu =	7.3	cm	0.61	16.83	
Incr.-deflection(Util)	df =	6.0	cm	1.00	16.83	
Prc.:Shear reinf (web)	asw =	5.00	cm ² /m	1.00	29.16	
Concrete strut capacity	$\eta =$	1.58		0.63	30.08	

---- Check not required

**** Check not fulfilled

Prc.:Precast member Add.: in-situ supplement

IS : Installed state SC : State of construction

AsDuk:Ductility reinforcement

Linear creep limit, informative:		Extrem		Utilisation	x [m]
Prc.:lin. creep t0(Sto)	$\sigma_c =$	-23.09	N/mm ²	1.41	0.80
Prc.:Compression quasi-permanent Lc	$\sigma_c =$	-19.11	N/mm ²	0.85	1.00
Tensile stress state I, informative:		Extrem		Utilisation	x [m]
Prc.:Tens.stress (IS)	$\sigma_t =$	9.52	N/mm ²	2.34	10.14
Prc.:Tens.stress (SC)	$\sigma_t =$	3.01	N/mm ²	1.19	0.80



Internal forces ULS [kN,kNm]

x [m]	Design sit. permanent/transient				from prestressing (formwork state)				
	Min My	Max My	Min Qz	Max Qz	Sto.tA Nv	Sto.tA Mv	Use.tE Nv	Use.tE Mv	PRE Deg
0.00	0.00	0.00	0.0	0.0	0.0	0.00	0.0	0.00	0.00
0.15	-0.10	-0.07	-1.3	-1.0	-300.0	-113.15	75.2	-16.91	2.41
0.15	-0.10	0.43	-1.3	460.8	-305.6	-115.28	72.7	-17.94	2.26
0.80	-2.83	293.41	-7.1	442.2	-1951.4	-771.31	-787.4	-359.95	1.66
1.00	-4.43	381.28	-8.9	436.5	-1956.7	-784.23	-1001.6	-467.11	2.00
1.35	-8.10	532.27	-12.1	426.4	-1956.7	-803.11	-1225.3	-591.58	2.30
1.36	-8.22	536.53	-12.2	426.1	-1956.7	-803.65	-1225.8	-592.43	2.28
3.37	-51.67	1334.23	-31.3	367.5	-1956.7	-911.27	-1317.2	-752.12	1.15
3.75	-64.26	1471.73	98.4	356.2	-1956.7	-931.47	-1327.8	-779.14	1.08
6.73	197.38	2400.70	75.4	266.8	-1956.7	-1088.60	-1386.4	-974.98	0.82
10.10	406.74	3125.02	46.9	162.5	-1956.7	-1263.95	-1416.4	-1164.27	0.75
11.15	451.87	3278.28	37.5	129.3	-1956.7	-1318.17	-1420.4	-1216.76	0.74
13.47	515.66	3492.30	15.8	54.9	-1956.7	-1437.39	-1423.1	-1322.50	0.76
15.15	529.63	3538.52	-0.7	0.7	-1956.7	-1523.27	-1420.7	-1390.67	0.79
16.83	515.66	3492.30	-54.9	-15.8	-1956.7	-1437.39	-1423.1	-1322.50	0.76
20.20	406.76	3125.02	-162.5	-46.9	-1956.7	-1263.95	-1416.4	-1164.27	0.75
23.57	197.39	2400.70	-266.8	-75.4	-1956.7	-1088.60	-1386.4	-974.98	0.82
26.55	-64.22	1471.73	-356.2	35.0	-1956.7	-931.47	-1327.8	-779.14	1.08
26.93	-51.64	1334.23	-367.5	31.2	-1956.7	-911.27	-1317.2	-752.12	1.15
28.94	-8.21	536.53	-426.1	12.2	-1956.7	-803.65	-1225.8	-592.43	2.28
28.95	-8.09	532.27	-426.4	12.1	-1956.7	-803.11	-1225.3	-591.58	2.30
29.16	-5.76	442.10	-432.4	10.2	-1956.7	-791.79	-1149.6	-543.73	2.35
30.08	-0.21	32.11	-458.8	1.9	-481.2	-182.49	-12.7	-52.60	1.61
30.15	-0.10	0.43	-460.8	1.3	-305.6	-115.28	72.7	-17.94	2.26
30.15	-0.10	-0.07	1.0	1.3	-300.0	-113.15	75.2	-16.91	2.41
30.30	0.00	0.00	0.0	0.0	0.0	0.00	0.0	0.00	0.00

Internal forces SLS

x [m]	<- char. Lc->		<- freq. Lc->		<q.- perm. Lc>	
	Min My	Max My	Min My	Max My	Min My	Max My
0.00	0.00	0.00	0.00	0.00	0.00	0.00
0.15	-0.07	-0.07	-0.07	-0.07	-0.07	-0.07
0.15	-0.07	0.32	-0.07	0.26	-0.07	0.24
0.80	-2.10	226.11	-2.10	190.39	-2.10	182.18
1.00	-3.28	293.83	-3.28	247.44	-3.28	236.78
1.35	-6.00	410.22	-6.00	345.50	-6.00	330.64
1.36	-6.09	413.50	-6.09	348.27	-6.09	333.29
3.37	-38.27	1028.49	-38.27	867.02	-38.27	829.94
3.75	-47.60	1134.52	-47.60	956.56	-47.60	915.69
6.73	214.02	1851.08	214.02	1562.52	214.02	1496.25
10.10	423.39	2410.09	423.39	2036.53	423.39	1950.74
11.15	468.52	2528.41	468.52	2137.06	468.52	2047.19
13.47	532.31	2693.69	532.31	2277.66	532.31	2182.13
15.15	546.28	2729.40	546.28	2308.09	546.28	2211.34
16.83	532.31	2693.69	532.31	2277.66	532.31	2182.13
20.20	423.40	2410.09	423.40	2036.53	423.40	1950.74
23.57	214.04	1851.08	214.04	1562.52	214.04	1496.25
26.55	-47.57	1134.52	-47.57	956.56	-47.57	915.69
26.93	-38.25	1028.49	-38.25	867.02	-38.25	829.94
28.94	-6.08	413.50	-6.08	348.27	-6.08	333.29
28.95	-5.99	410.22	-5.99	345.50	-5.99	330.64
29.16	-4.26	340.71	-4.26	286.93	-4.26	274.59
30.08	-0.16	24.73	-0.16	20.81	-0.16	19.91
30.15	-0.07	0.32	-0.07	0.26	-0.07	0.24
30.15	-0.07	-0.07	-0.07	-0.07	-0.07	-0.07
30.30	0.00	0.00	0.00	0.00	0.00	0.00



x[m]	<Flex. capacity>		<----resisting tensile force----->					
	η_{bo} = M_{Rd}/M_{Ed}	η_{to} = M_{Rd}/M_{Ed}	η_{bo} = T_{Rd}/T_{Ed}	σ/σ_R [N/mm ²]	al [cm]	η_{to} = T_{Rd}/T_{Ed}	σ/σ_R [N/mm ²]	al [cm]
0.00	---	---	---	0.00#	---	---	0.00#	---
0.08	---	---	---	0.00#	---	438.69	0.00#	43.0
0.15	---	---	---	0.00#	---	344.37	0.00#	43.2
0.15	---	---	0.86	0.00#	103.7	342.39	0.00#	43.2
0.20	88.35	---	1.01	0.00#	103.9	291.79	0.00#	43.3
0.40	18.09	699.13	1.53	0.00#	105.1	136.69	0.00#	43.8
0.60	10.31	283.22	1.94	0.00#	106.2	74.87	3.09*!	44.3
0.80	7.27	118.53	2.25	0.00#	107.3	48.00	4.18*!	44.8
1.00	5.67	76.13	2.54	0.00#	108.4	36.30	4.22*!	45.3
1.20	4.71	53.14	2.54	1.59#	109.5	28.21	4.26*!	45.8
1.35	4.20	42.15	2.41	1.50#	110.3	23.76	4.29*!	46.1
1.36	4.17	41.54	2.40	1.49#	110.4	23.50	4.29*!	46.2
1.40	4.05	40.52	2.37	1.47#	110.6	23.00	4.30*!	46.3
1.60	3.58	32.15	2.23	1.11#	111.7	18.93	4.34*!	46.8
1.80	3.22	25.55	2.10	1.03#	112.8	15.47	4.38*!	47.3
2.00	2.90	20.81	1.99	0.97#	114.0	13.08	4.43*!	47.8
3.37	1.92	8.15	1.63	5.93*!	121.6	7.67	4.83*!	51.1
3.75	1.79	6.64	1.56	7.51*!	123.7	6.64	4.97*!	96.0
6.73	1.30	---	1.26	15.14*!	88.6	---	0.02#	---
10.10	1.17	---	1.17	17.18*!	70.7	---	0.00#	---
11.15	1.17	---	1.17	16.94*!	73.3	---	0.00#	---
13.47	1.22	---	1.20	15.42*!	79.0	---	0.00#	---
16.83	1.22	---	1.21	15.42*!	79.0	---	0.00#	---
20.20	1.17	---	1.17	17.18*!	70.7	---	0.00#	---
23.57	1.30	---	1.26	15.14*!	88.6	---	0.02#	---
26.55	1.79	6.65	1.56	7.51*!	123.7	6.65	4.97*!	52.1
26.93	1.92	8.16	1.63	5.93*!	121.6	7.58	4.83*!	51.1
28.30	2.90	20.83	1.99	0.97#	114.0	13.09	4.43*!	47.8
28.50	3.22	25.58	2.10	1.03#	112.8	15.48	4.38*!	47.3
28.70	3.58	32.19	2.23	1.11#	111.7	18.95	4.34*!	46.8
28.90	4.05	40.58	2.37	1.47#	110.6	23.02	4.30*!	46.3
28.94	4.17	41.60	2.40	1.49#	110.4	23.53	4.29*!	46.2
28.95	4.20	42.21	2.41	1.50#	110.3	23.78	4.29*!	46.1
29.10	4.71	53.23	2.54	1.59#	109.5	28.25	4.26*!	45.8
29.30	5.67	76.28	2.54	0.00#	108.4	36.35	4.22*!	45.3
29.50	7.27	118.81	2.25	0.00#	107.3	48.07	4.18*!	44.8
29.70	10.31	284.02	1.94	0.00#	106.2	75.01	3.09*!	44.3
29.90	18.09	701.62	1.53	0.00#	105.1	136.99	0.00#	43.8
30.10	88.35	---	1.01	0.00#	103.9	292.58	0.00#	43.3
30.15	---	---	0.86	0.00#	103.7	343.36	0.00#	43.2
30.15	---	---	---	0.00#	---	345.35	0.00#	43.2
30.22	---	---	---	0.00#	---	440.04	0.00#	43.0
30.30	---	---	---	0.00#	---	---	0.00#	---

---- Check not required

**** Check not fulfilled

#:Main tens.stress σ !: σ > fctk0.05

*:Edge tens. str. σ_R !: σ_R > fctk0.05

Concrete stresses precast

x [m]	$\sigma_{c,1}$ [N/mm ²]	$\sigma_{c,2}$ [N/mm ²]	$\sigma_{c,Cc}$ [N/mm ²]	$\sigma_{c,Qc}$ [N/mm ²]	$\sigma_{t,Cc}$ [N/mm ²]	$\sigma_{t,SC}$ [N/mm ²]
0.08	-1.56	-1.56	-0.82	-0.82	1.52	0.34
0.15	-3.76	-3.76	-2.87	-2.87	0.92	0.67
0.15	-3.83	-3.83	-2.94	-2.93	0.92	0.68
0.68	-18.93	-22.44	-16.91	-16.91	1.14	2.56
0.80	-23.09	-26.50	-15.49	-15.49	1.21	3.01
0.83	-23.02	-26.57	-15.35	-15.35	1.11	2.97
1.00	-21.70	-26.55	-19.11	-19.11	0.50	2.71
1.14	-21.28	-26.55	-19.80	-18.63	0.01	2.50



x [m]	$\sigma_{c,1}$ [N/mm ²]	$\sigma_{c,2}$ [N/mm ²]	$\sigma_{c,Cc}$ [N/mm ²]	$\sigma_{c,Qc}$ [N/mm ²]	$\sigma_{t,Cc}$ [N/mm ²]	$\sigma_{t,SC}$ [N/mm ²]
1.35	-20.67	-26.55	-21.05	-18.08	---	2.21
1.36	-20.64	-26.55	-21.06	-18.05	---	2.19
3.37	-16.00	-27.10	-22.61	-14.17	0.56	4.68
3.75	-15.31	-27.31	-22.83	-13.56	1.77	4.78
6.73	-11.52	-17.59	-16.23	-10.16	7.72	2.28
10.10	-9.48	-14.30	-15.81	-10.67	9.52	1.03
13.47	-8.85	-12.78	-14.49	-9.69	8.44	0.81
15.15	-8.88	-12.46	-13.01	-8.71	7.25	0.96
16.83	-8.85	-12.78	-14.49	-9.69	8.44	0.81
20.20	-9.48	-14.30	-15.81	-10.67	9.52	1.03
23.57	-11.52	-17.59	-16.23	-10.16	7.72	2.28
26.55	-15.31	-27.31	-22.83	-13.56	1.77	4.78
26.93	-16.00	-27.10	-22.61	-14.17	0.56	4.68
28.94	-20.64	-26.55	-21.06	-18.05	---	2.19
28.95	-20.67	-26.55	-21.05	-18.08	---	2.21
29.16	-21.28	-26.55	-19.80	-18.63	0.01	2.50
29.30	-21.70	-26.55	-19.11	-19.11	0.50	2.71
29.47	-23.02	-26.57	-15.35	-15.35	1.11	2.97
29.50	-23.09	-26.50	-15.49	-15.49	1.21	3.01
29.62	-18.93	-22.44	-16.91	-16.91	1.14	2.56
30.15	-3.83	-3.83	-2.94	-2.93	0.92	0.68
30.15	-3.76	-3.76	-2.87	-2.87	0.92	0.67
30.22	-1.56	-1.56	-0.82	-0.82	1.52	0.34

---- Check not required

**** Check not fulfilled

$\sigma_{c,1}$: Compression and disproportional creeping check with early strength (storage)

$\sigma_{c,2}$: Compressive stress check with early strength (erection)

$\sigma_{c,Cc}$: Compression check Characteristic load combination

$\sigma_{c,Qc}$: Disproportional creep check quasi-perm. load combination

$\sigma_{t,Cc}$: Tensile stresses ,Installed state, Characteristic load combination (informative)

$\sigma_{t,SC}$: Tensile stresses,State of construction (informative)

Check the limit deformation:

Total sagging	$f \leq L/250$	Increase deflection	$ df \leq L/500$
Cantilever left	$f \leq 0.1 \text{ cm}$		$ df \leq 0.1 \text{ cm}$
Span	$f \leq 12.0 \text{ cm}$		$ df \leq 6.0 \text{ cm}$
Cantilever right	$f \leq 0.1 \text{ cm}$		$ df \leq 0.1 \text{ cm}$

quasi- permanent combination and eff. char. prestress

Deflection due to shrinkage considered

Tension stiffening: Member rigidity, Characteristic combination

	Storage		Utilization		
x [m]	ftA [cm]	ftE [cm]	ftA [cm]	ftE [cm]	df [cm]
0.00	0.0	0.1	-0.0	-0.1	-0.1
3.37	-0.9	-1.2	0.3	2.4	2.1
6.73	-1.4	-1.9	0.8	4.8	4.0
10.10	-1.7	-2.3	1.2	6.6	5.4
13.47	-1.8	-2.5	1.4	7.3	6.0
16.83	-1.8	-2.5	1.4	7.3	6.0
20.20	-1.7	-2.3	1.2	6.6	5.4
23.57	-1.4	-1.9	0.8	4.8	4.0
26.93	-0.9	-1.2	0.3	2.4	2.1
30.30	0.0	0.1	-0.0	-0.1	-0.1
$ df = ftE(\text{service}) - ftA(\text{service})$					



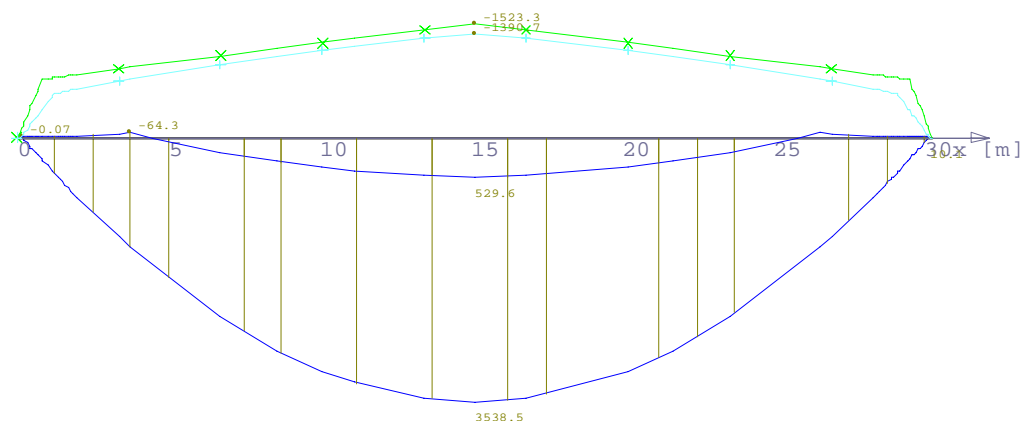
Shear resistance

x [m]	V _{Ed} [kN]	V _{Ed,red} [kN]	cotθ	z [cm]	asw,Web [cm ² /m]	η = V _{Rd,max} /V _{Ed}
0.08	0.7	----	1.00	58.4	2.15	---
0.22	456.5	----	2.50*	68.9	5.00	1.58
0.23	455.9	----	2.50*	69.1	5.00	1.59
1.14	402.9	402.9	2.50	74.2	5.00	2.15
1.35	391.4	391.4	2.50	75.3	4.78	2.26
1.36	390.8	390.8	2.50	75.3	4.77	2.27
3.37	289.9	289.9	2.50	85.2	3.13	2.65
3.75	272.4	272.4	2.50	86.9	2.88	3.09
6.73	149.8	149.8	1.58	101.6	2.15	10.40
10.10	41.0	41.0	1.00	118.5	2.15	41.18
13.47	73.4	73.4	1.00	134.8	2.15	30.71
15.15	122.4	122.4	1.00	143.1	2.15	19.47
16.83	73.4	73.4	1.00	134.8	2.15	30.71
20.20	41.0	41.0	1.00	118.5	2.15	41.18
23.57	149.8	149.8	1.58	101.6	2.15	10.40
26.55	272.4	272.4	2.50	86.9	2.88	3.09
26.93	289.9	289.9	2.50	85.2	3.13	2.65
28.94	390.8	390.8	2.50	75.3	4.77	2.27
28.95	391.4	391.4	2.50	75.3	4.78	2.26
29.16	402.9	402.9	2.50	74.2	5.00	2.15
30.08	456.5	----	2.50*	68.9	5.00	1.58
30.22	0.7	----	1.00	58.4	2.15	---

---- Check not required
 **** Check not fulfilled
 *: Take over from last construction phase

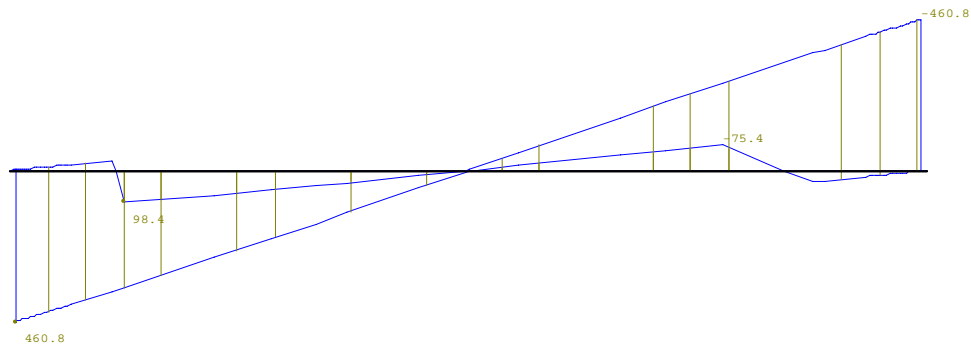
Internal forces

- max M_{Ed} from external loads (PT)
- min M_{Ed} from external loads (PT)
- × Moment from prestressing, t= t_A storage
- + Moment from prestressing, t= t_E use



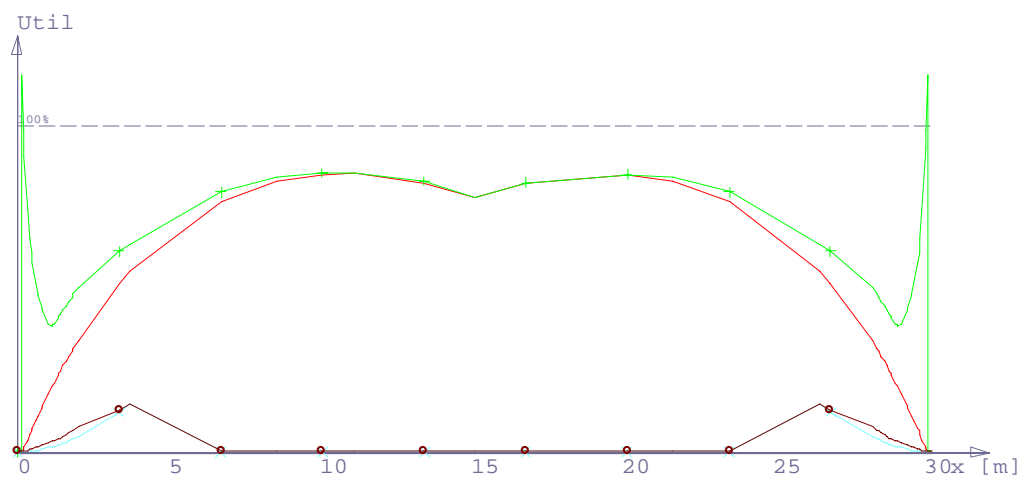


max VEd from external loads (PT)
min VEd from external loads (PT)



Bending resistance (failure safety)

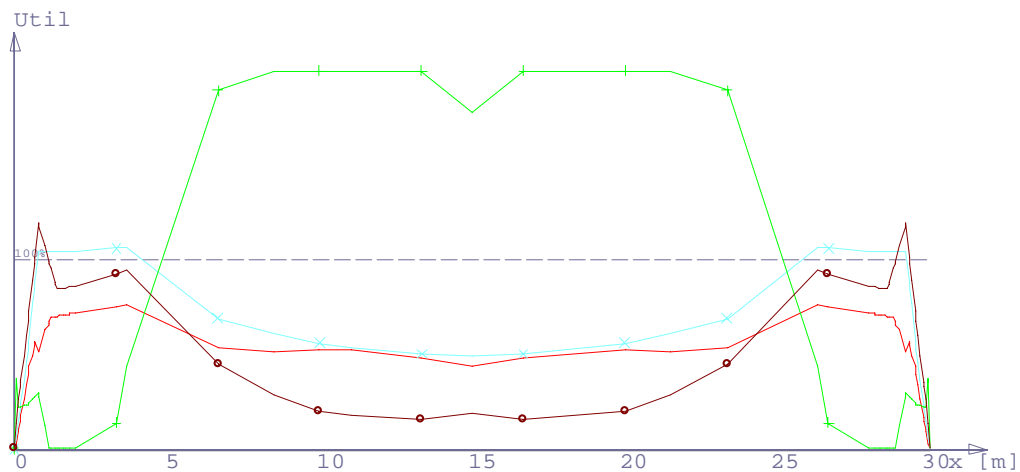
— Flexural capacity bottom	$\eta = 1.17$	$x = 19.53 \text{ m}$
x Flexural capacity top	$\eta = 6.64$	$x = 3.75 \text{ m}$
+ Resisting tens force bot	$\eta = 0.86$	$x = 30.15 \text{ m}$
o Resisting tens force top	$\eta = 6.64$	$x = 3.75 \text{ m}$





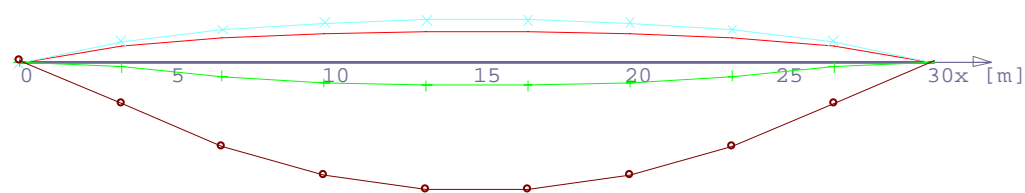
Ultimate stress precast component

—	Prc.:Compr.stress Cc	$\sigma_c = -22.83 \text{ N/mm}^2$ x= 3.75 m
×	Prc.:Compr.stress t0(sto)	$\sigma_c = -27.31 \text{ N/mm}^2$ x= 3.75 m
+	Prc.:Tens.stress (IS)	> 100% condition II, informative only
●	Prc.:Tens.stress (SC)	> 100% condition II, informative only



Deformation

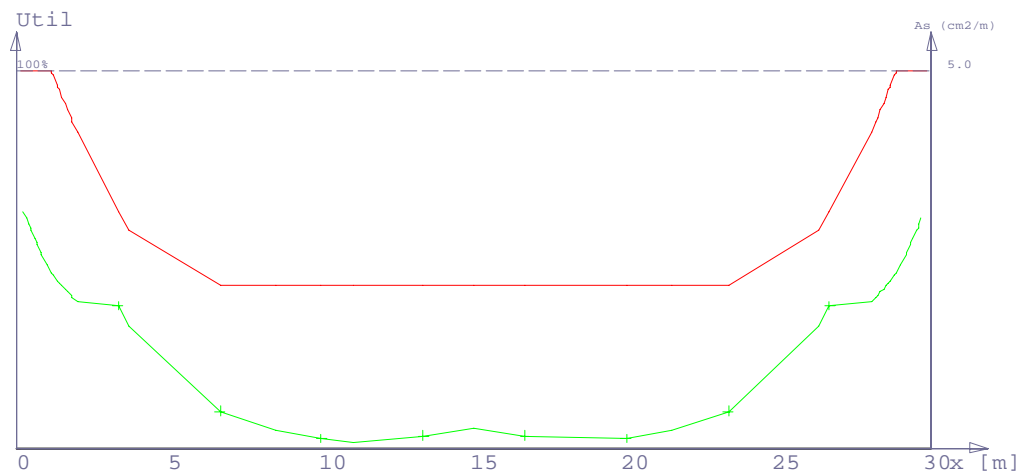
—	Sagging	t=tA storage	-1.83 cm
×	Sagging	t=tE storage	-2.45 cm
+	Sagging	t=tA utilisatio	1.36 cm
●	Sagging	t=tE utilisatio	7.34 cm





Shear force resistance (shear covering)

————— Prc.:Shear reinf (web) $a_{sw} = 5.00 \text{ cm}^2/\text{m}$ $x=29.16 \text{ m}$
+————— Concrete strut capacity $\eta = 1.58$ $x=30.08 \text{ m}$



Selected section $x = 11.00 \text{ m}$ from left support

Internal force combinations from external loading

LAc: dominant variable action (leading action)

ULS-PT: permanent + transient design situation (fundam. combination)

SLS-Cc: characteristic combination

SLS-Fc: frequent combination

SLS-Qc: quasi-permanent combination

maximum moment : [kNm]

	ULS-PT	SLS-Cc	SLS-Fc	SLS-Qc
Storage	1240.12	918.59	918.59	918.59
Storage/Erection	649.16	468.52	468.52	468.52
Utilization	3278.28	2528.41	2137.06	2047.19
LAc	10	10	10	-

Minimum moment : [kNm]

	ULS-PT	SLS-Cc	SLS-Fc	SLS-Qc
Storage	918.56	918.59	918.59	918.59
Storage/Erection	451.87	468.52	468.52	468.52
Utilization	2047.16	2047.19	2047.19	2047.19
LAc	-	-	-	-

maximum shear force:[kN]

	ULS-PT
Storage	51.6
Storage/Erection	52.4
Utilization	129.3
LAc	10



Effective Tendons (prestressed formwork state for $t = t_0$ (sto))

Layer No.	No.	Area [cm ²]	Distance f.bottom [cm]	Prestress		tens.force		Shorttime Relaxation [N/mm ²]
				max [N/mm ²]	min [N/mm ²]	max [kN]	min [kN]	
1	3	2.8	8.5	956.37	956.37	266.8	266.8	-4.63
2	3	2.8	12.3	956.37	956.37	266.8	266.8	-4.63
3	3	2.8	16.1	956.37	956.37	266.8	266.8	-4.63
4	3	2.8	19.9	956.37	956.37	266.8	266.8	-4.63
5	3	2.8	23.7	956.37	956.37	266.8	266.8	-4.63
6	3	2.8	27.5	956.37	956.37	266.8	266.8	-4.63
7	3	2.8	31.3	956.37	956.37	266.8	266.8	-4.63
8	1	0.9	35.1	956.37	956.37	88.9	88.9	-4.63

$\Delta\sigma(Tt_0) = -39$ N/mm² due to heat treatment

Untensioned reinforcement

Layer	Number	Diameter [mm]	Area [cm ²]	LE [cm]
1	2	16	4.0	3.6
2	2	20	6.3	135.2
3	2	20	6.3	146.4

Cross-section Precast :

Layer of cross-section from top to bottom			
Nr	Width [cm]	Distance [cm]	Remarks
1	60.0	0.0	Web begin Web end
2	60.0	15.0	
3	19.0	23.2	
4	19.0	150.2	

Cross-section Values

	brutto			ideal		
	A _c [cm ²]	z _u [cm]	I _c [cm ⁴]	A _i [cm ²]	z _i [cm]	I _i [cm ⁴]
Precast cross-section	3636.9	89.2	8019344	3797.3	88.0	8768771

Internal forces from prestress (mean values, prestressed formwork state)

Creep period	N _{pm} ⁽⁰⁾		M _{pm} ⁽⁰⁾	
	tB [kN]	tE [kN]	tB [kNm]	tE [kNm]
Storage	-1956.7	-1793.6	-1318.17	-1254.74
Utilization	-1793.6	-1420.4	-1254.74	-1216.76

tA=Begin, tE=End creep period

Prestress steel relaxation		
Lay. No.	Storage $\Delta\sigma_{p,r1}$ [N/mm ²]	Utilization $\Delta\sigma_{p,r2}$ [N/mm ²]
1	-0.10	-13.00
2	-0.10	-12.94
3	-0.11	-12.89
4	-0.11	-12.84
5	-0.11	-12.79
6	-0.11	-12.73
7	-0.11	-12.68
8	-0.11	-12.63



Prestr. steel, losses due to creeping, shrinking and relaxation:		
Lay. No.	Storage $\Delta\sigma_{p,csr1}^{(0)}$ [N/mm ²]	Utilization $\Delta\sigma_{p,csr2}^{(0)}$ [N/mm ²]
1	-50.61	-75.05
2	-50.09	-77.17
3	-49.57	-79.29
4	-49.05	-81.41
5	-48.54	-83.53
6	-48.02	-85.65
7	-47.50	-87.77
8	-46.98	-89.89

Stress in rebars due to creeping,shrinking and relaxation:		
Lay. No.	Storage $\Delta\sigma_{s,csr1}^{(0)}$ [N/mm ²]	Utilization $\Delta\sigma_{s,csr2}^{(0)}$ [N/mm ²]
1	-52.51	-63.45
2	-34.06	-140.25
3	-32.50	-146.79

Bending with Normal Force ULS

L.	Creep period	Cross-section	Tens-zone	z [cm]	M _{Rd} [kNm]	M _{Ed} [kNm]	η (>1.0)	
1	tB Storage	P	top	119.4	634.58	MEd < 0	n/a	#1
2	tE Storage	P	bottom	123.7	3829.99	1240.12	3.09	
3	tB Storage/Erection	P	top	119.4	634.58	MEd < 0	n/a	#1
4	tE Storage/Erection	P	bottom	123.7	3829.99	649.16	5.90	
5	tE Utilization	P	top	125.0	781.51	MEd < 0	n/a	
6	tE Utilization	P	bottom	123.4	3843.82	3278.28	1.17	

#1: fck(t) = 0.73 * fck

Interim results : Ultimate elongation and internal forces										
L.	ε _c [‰]	ε _s [‰]	x [cm]	Ap [cm ²]	As [cm ²]	Zp [kN]	Zs [kN]	Dc [kN]	Dp [kN]	Ds [kN]
1	3.500	5.500	56.9	0.0	12.6	0.0	549.1	1807.6	-1441.6	166.9
2	3.500	21.900	20.2	20.5	4.0	2962.2	180.5	2730.3	0.0	380.1
3	3.500	5.500	56.9	0.0	12.6	0.0	549.1	1807.6	-1441.6	166.9
4	3.500	21.900	20.2	20.5	4.0	2962.2	180.5	2730.3	0.0	380.1
5	3.500	9.500	39.4	0.0	12.6	0.0	551.9	1717.7	-1308.2	163.9
6	3.500	22.700	19.6	20.5	4.0	2967.4	180.7	2660.2	0.0	468.0

Shear Resistance

Design value shear force						
L.	Creep period	Combination	V _{Ed,0} [kN]	M _{Ed} [kNm]	dV [kN]	due to
1	tB Storage	QMax	51.6	1240.10	-49.6	Vccd
2	tE Storage	QMax	51.6	1240.10	-49.6	Vccd
3	tB Storage/Erection	QMax	52.4	637.91	-25.5	Vccd
4	tE Storage/Erection	QMax	52.4	637.91	-25.5	Vccd
5	tB Utilization	MMax	129.3	3278.28	-131.5	Vccd
6	tE Utilization	MMax	129.3	3278.28	-131.5	Vccd



Effective cross-section									
L.	Cross-section	Tens-zone	b _w [cm]	d [cm]	z [cm]	A _c [cm ²]	A _{sl} [cm ²]	σ _{cd} [N/mm ²]	V _{Rdc} [kN]
1	P	bottom	19.0	146.6	123.7	3636.9	24.5	4.84	347.6
2	P	bottom	19.0	146.6	123.7	3636.9	24.5	4.44	347.0
3	P	bottom	19.0	146.6	123.7	3636.9	24.5	4.84	347.6
4	P	bottom	19.0	146.6	123.7	3636.9	24.5	4.44	347.0
5	P	bottom	19.0	146.6	123.4	3636.9	24.5	4.44	347.0
6	P	bottom	19.0	146.6	123.4	3636.9	24.5	3.52	308.4

Shear design v ₁ = 0.480									
L.	V _{Ed} [kN]	V _{Ed,red} [kN]	a _{cw}	cotθ	asw [cm ² /m]	Note	a _j [cm]	V _{Rd,max} [kN]	
1	2.0	2.0	1.199	1.000	1.83	Min	73.3	1754.2	#1
2	2.0	2.0	1.133	1.000	2.15	Min	73.3	2130.3	
3	26.8	26.8	1.199	1.000	1.83	Min	73.3	1754.2	#1
4	26.8	26.8	1.133	1.000	2.15	Min	73.3	2130.3	
5	2.2	2.2	1.133	1.000	2.15	Min	73.3	2125.8	
6	2.2	2.2	1.105	1.000	2.15	Min	73.3	2073.9	

#1: f_{ck}(t) = 0.73 * f_{ck}

Check of crack width limit in SLS

perm. crack width: w_k < 0 mm, Frequent load combination

L.	Creep period	Cross-section	Tens-zone	r _{sub} r _{inf}	max.σ _s [N/mm ²]	S _{r,max} [mm]	ε _{sm} -ε _{cm} [‰]	w _k [mm]
1	tB Storage	P	top	1.00	CS completely compressed			
2	tE Storage	P	bottom	1.00	CS completely compressed			
3	tB Storage/Erection	P	top	1.00	no cracks			
4	tE Storage/Erection	P	bottom	1.00	CS completely compressed			
5	tE Utilization	P	top	1.00	CS completely compressed			
6	tE Utilization	P	bottom	1.00	128.75	206	0.386	0

Internal forces and elongation								
L.	N _{des} [kN]	M _{des} [kNm]	max.σ [N/mm ²]	State I XOI [cm]	State II φ _{eff}	State II ε _c [‰]	State II XOII [cm]	
1	-1956.7	-399.59	-2.32	201.0				
2	-1793.6	-336.16	-8.10	211.2				
3	-1956.7	-849.65	0.88	141.1				
4	-1793.6	-786.22	-12.61	140.6				
5	-1420.4	830.43	-9.64	101.7				
6	-1420.4	920.30	5.49	97.9	1.78	-0.775	80.1	

XOI: Pressure zone height in state I XOII: Pressure zone height in state II

L.	h _{c,ef} [cm]	A _{ceff} [cm ²]	ξ ₁	A _p [cm ²]	A _s [cm ²]	ρ _{p,ef} [%]	ρ _{tot} [%]	k1	k2	k3	c [cm]	k4
6	23.4	444.1	1.15	11.2	4.0	4.257	3.418	1.38	0.50	3.40	2.8	0.425

Internal forces cracking and strains (state II)								
L.	N _{des} [kN]	M _{des} [kNm]	max.σ [N/mm ²]	State I XOI [cm]	State II φ _{eff}	State II ε _c [‰]	State II XOII [cm]	
6	-1420.4	778.83	4.07	104.4				

XOI: Pressure zone height in state I XOII: Pressure zone height in state II



Minimum reinforcement for crack control:

L.	Creep period	Cross-section	Tens-zone	r_{sup} r_{inf}	σ_t [N/mm ²]	req. As [cm ²]	exist. As [cm ²]
1	tB Storage	P	top	1.00	-1.89	< 4.07	not req.
2	tE Storage	P	bottom	1.00	-8.10	< 4.07	not req.
3	tB Storage/Erection	P	top	1.00	1.31	< 4.07	not req.
4	tE Storage/Erection	P	bottom	1.00	-12.61	< 4.07	not req.
5	tE Utilization	P	top	1.00	-9.37	< 4.07	not req.
6	tE Utilization	P	bottom	1.00	9.42	<= 0 cm ²	

L.	D [mm]	x0IZ [cm]	A _p [cm ²]	ξ_1	k	k _c	A _{ct} [cm ²]	Web A _s [cm ²]	Flange k	k _c	A _{ct} [cm ²]	A _s [cm ²]
6	16	45.8	5.6	1.15	0.65	0.29	871.0	4.3	--no flange--			

x0IZ: tensile zone in state I due to cracking forces

Ductility reinforcement in precompressed tensile zone:

b [cm ³]	f _{ctm} [N/mm ²]	Z _s [cm]	req. As [cm ²]	exist. As [cm ²]
19	4.07	146.6	5.9	4.0

Stress checks SLS

Concrete edge stresses in state I due to prestress, creep, shrinkage and relaxation			
L.	due to	top [N/mm ²]	bottom [N/mm ²]
1	Prestr. release anchorage	4.20	-18.38
2	csr storage	-0.02	1.07
3	csr utilisation	0.71	1.36

Tab. Compr stresses of concrete					
L.	Creep period	Cross-section	M _{Ed} + = Max - = Min	Cc,Pk [N/mm ²]	σ _c Precast Qc,Pk [N/mm ²]
1	tB Storage	P	--	-9.16	-9.16
2	tE Storage	P	--	-8.10	-8.10
3	tB Storage/Erection	P	--	-13.68	
4	tE Storage/Erection	P	--	-12.61	
5	tB Utilization	P	+-	-15.68	-10.57
6	tE Utilization	P	+-	-14.19	-9.53

Tab. Steel- and Concrete tension stress						
L.	Creep period	Cross-section	M _{Ed} + = Max - = Min	σ _b Cc,Pm [N/mm ²]	σ _s Cc,Pk [N/mm ²]	σ _t Cc,Pk [N/mm ²]
1	tB Storage	P	+-	916.52	< 0	ZII
2	tE Storage	P	+-	873.82	< 0	ZII
3	tB Storage/Erection	P	---	902.22	2.76	0.88
4	tE Storage/Erection	P	+-	859.52	< 0	0.86
5	tB Utilization	P	++	1067.66	124.02	ZII
6	tE Utilization	P	++	1068.31	142.41	ZII

Pk= Prestres char. value, Pm= prestress mean value, Still: State II

Selected section x = 1.00 m from left support

Internal force combinations from external loading

LAC: dominant variable action (leading action)

ULS-PT : permanent + transient design situation (fundam. combination)

SLS-Cc : characteristic combination

SLS-Fc : frequent combination

SLS-Qc : quasi-permanent combination



maximum moment : [kNm]

	ULS-PT	SLS-Cc	SLS-Fc	SLS-Qc
Storage	162.93	120.67	120.67	120.67
Storage/Erection	-4.35	-4.35	-4.35	-4.35
Utilization	446.42	344.04	289.74	277.27
LAc	10	10	10	-

Minimum moment : [kNm]

	ULS-PT	SLS-Cc	SLS-Fc	SLS-Qc
Storage	120.65	120.67	120.67	120.67
Storage/Erection	-5.87	-4.35	-4.35	-4.35
Utilization	277.25	277.27	277.27	277.27
LAc	-	-	-	-

maximum shear force: [kN]

	ULS-PT
Storage	158.5
Storage/Erection	-10.3
Utilization	432.1
LAc	10

Effective Tendons (prestressed formwork state for t = t0 (sto))

Layer No.	No.	Area Ap [cm²]	Distance f.bottom [cm]	Prestress		tens.force		Shorttime Relaxation [N/mm²]
				max [N/mm²]	min [N/mm²]	max [kN]	min [kN]	
1	3	2.8	8.5	956.37	912.14	266.8	254.5	-4.63
2	3	2.8	12.3	956.37	912.14	266.8	254.5	-4.63
3	3	2.8	16.1	956.37	912.14	266.8	254.5	-4.63
4	3	2.8	19.9	956.37	912.14	266.8	254.5	-4.63
5	3	2.8	23.7	956.37	912.14	266.8	254.5	-4.63
6	3	2.8	27.5	956.37	912.14	266.8	254.5	-4.63
7	3	2.8	31.3	956.37	912.14	266.8	254.5	-4.63
8	1	0.9	35.1	956.37	912.14	88.9	84.8	-4.63

$\Delta\sigma(Tt0) = -39 \text{ N/mm}^2$ due to heat treatment

Untensioned reinforcement

Layer	Number	Diameter [mm]	Area [cm²]	LE [cm]
1	2	16	4.0	3.6
2	2	20	6.3	85.7
3	2	20	6.3	96.9

Cross-section Precast :

Layer of cross-section from top to bottom			
Nr	Width [cm]	Distance [cm]	Remarks
1	60.0	0.0	Web begin Web end
2	60.0	15.0	
3	19.0	23.2	
4	19.0	100.7	

Cross-section Values

	brutto			ideal		
	A _c [cm²]	z _u [cm]	I _c [cm⁴]	A _i [cm²]	z _i [cm]	I _i [cm⁴]
Precast cross-section	2696.3	62.2	2560641	2856.7	61.1	2848818



Internal forces from prestress (mean values, prestressed formwork state)

Creep period	$N_{pm}^{(0)}$		$M_{pm}^{(0)}$		φ_{Fak} Prc
	tB [kN]	tE [kN]	tB [kNm]	tE [kNm]	
Storage	-1956.7	-1637.6	-792.33	-674.94	1.22
Utilization	-1717.0	-1160.2	-707.67	-549.27	1.00

tA=Begin, tE=End creep period
 φ_{Fak} : Increase factor creep modulus (non-linear creep: > 1.0)

Prestress steel relaxation		
Lay. No.	Storage $\Delta\sigma_{p,r1}$ [N/mm ²]	Utilization $\Delta\sigma_{p,r2}$ [N/mm ²]
1	-0.08	-8.50
2	-0.08	-8.68
3	-0.09	-8.87
4	-0.09	-9.06
5	-0.09	-9.25
6	-0.09	-9.45
7	-0.09	-9.65
8	-0.10	-9.85

Prestr. steel, losses due to creeping, shrinking and relaxation:		
Lay. No.	Storage $\Delta\sigma_{p,csr1}^{(0)}$ [N/mm ²]	Utilization $\Delta\sigma_{p,csr2}^{(0)}$ [N/mm ²]
1	-93.48	-163.58
2	-90.24	-160.74
3	-86.99	-157.90
4	-83.75	-155.07
5	-80.51	-152.23
6	-77.27	-149.40
7	-74.03	-146.57
8	-70.79	-143.74

Stress in rebars due to creeping, shrinking and relaxation:		
Lay. No.	Storage $\Delta\sigma_{s,csr1}^{(0)}$ [N/mm ²]	Utilization $\Delta\sigma_{s,csr2}^{(0)}$ [N/mm ²]
1	-100.10	-164.76
2	-28.24	-98.51
3	-18.44	-89.47

Bending with Normal Force ULS

L.	Creep period	Cross-section	Tens-zone	z [cm]	M_{Rd} [kNm]	M_{Ed} [kNm]	η (>1.0)	
1	tB Storage	P	top	70.5	339.08	$M_{Ed} < 0$	n/a	#1
2	tE Storage	P	bottom	74.4	2207.63	162.93	13.55	
3	tB Storage/Erection	P	top	70.5	339.08	5.87	57.79	#1
4	tE Storage/Erection	P	bottom	74.4	2207.63	$M_{Ed} < 0$	n/a	
5	tB Utilization	P	top	75.1	496.04	$M_{Ed} < 0$	n/a	
6	tE Utilization	P	bottom	74.3	2193.79	446.42	4.91	

#1: $f_{ck}(t) = 0.73 \cdot f_{ck}$



Interim results : Ultimate elongation and internal forces										
L.	ϵ_c [‰]	ϵ_s [‰]	x [cm]	A _p [cm ²]	A _s [cm ²]	Z _p [kN]	Z _s [kN]	D _c [kN]	D _p [kN]	D _s [kN]
1	3.500	2.500	56.5	0.0	12.6	0.0	500.3	1794.5	-1443.3	166.9
2	3.500	13.900	19.5	20.5	4.0	2828.8	178.1	2654.0	0.0	365.7
3	3.500	2.500	56.5	0.0	12.6	0.0	500.3	1794.5	-1443.3	166.9
4	3.500	13.900	19.5	20.5	4.0	2828.8	178.1	2654.0	0.0	365.7
5	3.500	4.900	40.4	0.0	12.6	0.0	548.3	1759.4	-1403.1	163.9
6	3.500	14.700	18.7	20.5	4.0	2828.0	178.2	2551.6	0.0	419.9

Shear Resistance

Design value shear force						
L.	Creep period	Combination	V _{Ed,0} [kN]	M _{Ed} [kNm]	dV [kN]	due to
1	tB Storage	QMax	158.5	162.91	-10.8	V _{ccd}
2	tE Storage	QMax	158.5	162.91	-10.8	V _{ccd}
3	tB Storage/Erection	QMax	-10.3	-5.87	0.0	-----
4	tE Storage/Erection	QMax	-10.3	-5.87	0.0	-----
5	tB Utilization	QMax	432.1	446.40	-29.8	V _{ccd}
6	tE Utilization	QMax	432.1	446.40	-29.8	V _{ccd}

Effective cross-section									
L.	Cross-section	Tens-zone	b _w [cm]	d [cm]	z [cm]	A _c [cm ²]	A _{sl} [cm ²]	σ _{cd} [N/mm ²]	V _{Rdc} [kN]
1	P	bottom	19.0	97.1	74.4	2696.3	24.5	4.86	251.6
2	P	bottom	19.0	97.1	74.4	2696.3	24.5	5.47	281.6
3	P	top	19.0	91.3	70.5	2696.3	12.6	4.86	217.3
4	P	top	19.0	91.3	70.5	2696.3	12.6	5.47	243.3
5	P	bottom	19.0	97.1	74.3	2696.3	24.5	5.73	288.9
6	P	bottom	19.0	97.1	74.3	2696.3	24.5	3.87	237.5

Shear designv1 = 0.480									
L.	V _{Ed} [kN]	V _{Ed,red} [kN]	a _{cw}	cotθ	asw [cm ² /m]	Note	a _i [cm]	V _{Rd,max} [kN]	
1	147.7	147.7	1.250	2.487	1.83	Min	92.6	761.6	#1
2	147.7	147.7	1.164	2.123	2.15	Min	79.0	1015.3	
3	10.3	10.3	1.250	1.000	1.83	Min	45.6	1042.2	#1
4	10.3	10.3	1.164	1.000	2.15	Min	45.6	1247.5	
5	402.4	402.4	1.172	2.500	4.98	Var	92.8	912.3	
6	402.4	402.4	1.116	2.500	4.98	Var	92.8	868.9	

#1: f_{ck}(t) = 0.73 * f_{ck}

Check of crack width limit in SLS

perm. crack width: w_k < 0 mm, Frequent load combination

L.	Creep period	Cross-section	Tens-zone	r _{sub} r _{inf}	max.σ _s [N/mm ²]	S _{r,max} [mm]	ε _{sm} -ε _{cm} [‰]	w _k [mm]
1	tB Storage	P	top	1.00	no cracks			
2	tE Storage	P	bottom	1.00	CS completely compressed			
3	tB Storage/Erection	P	top	1.00	56.16	431	0.168	0
4	tE Storage/Erection	P	bottom	1.00	CS completely compressed			
5	tB Utilization	P	top	1.00	CS completely compressed			
6	tE Utilization	P	bottom	1.00	CS completely compressed			



Internal forces and elongation							
			State I		State II		
L.	N_{ges} [kN]	M_{ges} [kNm]	$\max.\sigma$ [N/mm ²]	XOI [cm]	φ_{eff}	ϵ_c [‰]	XOII [cm]
1	-1956.7	-671.66	2.49	90.1	0.00	-0.718	69.6
2	-1637.6	-554.27	-17.62	90.5			
3	-1956.7	-796.68	4.23	85.6			
4	-1637.6	-679.29	-20.30	85.1			
5	-1717.0	-430.40	-0.03	100.9			
6	-1160.2	-259.53	-9.63	105.7			

XOI: Pressure zone height in state I XOII: Pressure zone height in state II

L.	$h_{c,ef}$ [cm]	A_{ceff} [cm ²]	ξ_1	A_p [cm ²]	A_s [cm ²]	$\rho_{p,ef}$ [%]	ρ_{tot} [%]	k1	k2	k3	c [cm]	k4
3	10.4	621.0	1.29	0.0	6.3	1.012	1.012	0.80	0.50	3.40	2.8	0.425

Internal forces cracking and strains (state II)

			State I		State II		
L.	N_{ges} [kN]	M_{ges} [kNm]	$\max.\sigma$ [N/mm ²]	XOI [cm]	φ_{eff}	ϵ_c [‰]	XOII [cm]
3	-1956.7	-785.48	4.07	85.9			

XOI: Pressure zone height in state I XOII: Pressure zone height in state II

Minimum reinforcement for crack control:

L.	Creep period	Cross-section	Tens-zone	r_{sub} r_{inf}	σ_t [N/mm ²]	req. A_s [cm ²]	exist. A_s [cm ²]
1	tB Storage	P	top	1.00	3.61	< 4.07 not req.	
2	tE Storage	P	bottom	1.00	-17.62	< 4.07 not req.	
3	tB Storage/Erection	P	top	1.00	5.34	<= 0 cm ²	
4	tE Storage/Erection	P	bottom	1.00	-20.30	< 4.07 not req.	
5	tB Utilization	P	top	1.00	1.92	< 4.07 not req.	
6	tE Utilization	P	bottom	1.00	-8.46	< 4.07 not req.	

					Web				Flange			
L.	D [mm]	xOIZ [cm]	A_p [cm ²]	ξ_1	k	k_c	A_{ct} [cm ²]	A_s [cm ²]	k	k_c	A_{ct} [cm ²]	A_s [cm ²]
3	20	14.8	0.0	0.00	0.65	0.00	280.6	-nan(ind)	0.97	0.53	498.5	4.8

xOIZ: tensile zone in state I due to cracking forces

Ductility reinforcement in precompressed tensile zone:

b [cm ³]	f_{ctm} [N/mm ²]	Zs [cm]	req. A_s [cm ²]	exist. A_s [cm ²]
19	4.07	97.1	3.9	4.0

Stress checks SLS

Concrete edge stresses in state I due to prestress, creep, shrinkage and relaxation			
		$\sigma_{R,Precast}$	
L.	due to	top [N/mm ²]	bottom [N/mm ²]
1	Prestr. release anchorage	4.17	-23.84
2	csr storage	-0.34	2.65
3	csr utilisation	-0.08	4.58



Tab. Compr stresses of concrete						
			M _{Ed}	σ _c Precast		
L.	Creep period	Cross-section	+ = Max - = Min	Cc,Pk [N/mm²]	Qc,Pk [N/mm²]	
1	tB Storage	P	--	-21.25	-21.25	#1
2	tE Storage	P	--	-18.60	-18.60	
3	tB Storage/Erection	P	--	-26.55*		
4	tE Storage/Erection	P	--	-19.98		
5	tB Utilization	P	--	-15.24	-15.24	
6	tE Utilization	P	--	-10.66	-10.66	
#1: due toσc > 0.45* fck(t) increased ceep modulus						

Tab. Steel- and Concrete tension stress						
L.	Creep period	Cross-section	M_{Ed} + = Max - = Min	σ_o $\sigma_{c,Pm}$ [N/mm ²]	σ_s $\sigma_{c,Pk}$ [N/mm ²]	σ_t $\sigma_{c,Pk}$ [N/mm ²]
1	tB Storage	P	---	887.99	8.61	2.49
2	tE Storage	P	+-	781.46	< 0	2.15
3	tB Storage/Erection	P	---	900.14	56.16	ZII
4	tE Storage/Erection	P	---	764.91	48.15	ZII
5	tB Utilization	P	++	836.43	< 0	ZII
6	tE Utilization	P	++	664.02	< 0	ZII
Pk= Prestres char. value, Pm= prestress mean value, StII: State II						

Selected section x = 3.60 m from left support

Internal force combinations from external loading

LAc: dominant variable action (leading action)

ULS-PT : permanent + transient design situation (fundam. combination)

SLS-Cc : characteristic combination

SLS-Fc : frequent combination

SLS-Qc : quasi-permanent combination

maximum moment : [kNm]

	ULS-PT	SLS-Cc	SLS-Fc	SLS-Qc
Storage	543.37	402.48	402.48	402.48
Storage/Erection	-47.60	-47.60	-47.60	-47.60
Utilization	1471.73	1134.52	956.56	915.69
LAc	10	10	10	-

Minimum moment : [kNm]

	ULS-PT	SLS-Cc	SLS-Fc	SLS-Qc
Storage	402.45	402.48	402.48	402.48
Storage/Erection	-64.26	-47.60	-47.60	-47.60
Utilization	915.67	915.69	915.69	915.69
LAc	-	-	-	-

maximum shear force:[kN]

	ULS-PT
Storage	133.8
Storage/Erection	134.5
Utilization	356.2
LAc	10



Effective Tendons (prestressed formwork state for $t = t_0$ (sto))

Layer No.	No.	Area [cm ²]	Distance f.bottom [cm]	Prestress		tens.force		Shorttime Relaxation [N/mm ²]
				max [N/mm ²]	min [N/mm ²]	max [kN]	min [kN]	
1	3	2.8	8.5	956.37	956.37	266.8	266.8	-4.63
2	3	2.8	12.3	956.37	956.37	266.8	266.8	-4.63
3	3	2.8	16.1	956.37	956.37	266.8	266.8	-4.63
4	3	2.8	19.9	956.37	956.37	266.8	266.8	-4.63
5	3	2.8	23.7	956.37	956.37	266.8	266.8	-4.63
6	3	2.8	27.5	956.37	956.37	266.8	266.8	-4.63
7	3	2.8	31.3	956.37	956.37	266.8	266.8	-4.63
8	1	0.9	35.1	956.37	956.37	88.9	88.9	-4.63

$\Delta\sigma(Tt_0) = -39$ N/mm² due to heat treatment

Untensioned reinforcement

Layer	Number	Diameter [mm]	Area [cm ²]	LE [cm]
1	2	16	4.0	3.6
2	2	20	6.3	98.6
3	2	20	6.3	109.8

Cross-section Precast :

Layer of cross-section from top to bottom			
Nr	Width [cm]	Distance [cm]	Remarks
1	60.0	0.0	Web begin Web end
2	60.0	15.0	
3	19.0	23.2	
4	19.0	113.6	

Cross-section Values

	brutto			ideal		
	A _c [cm ²]	z _u [cm]	I _c [cm ⁴]	A _i [cm ²]	z _i [cm]	I _i [cm ⁴]
Precast cross-section	2940.8	69.3	3618822	3101.3	68.2	4006279

Internal forces from prestress (mean values, prestressed formwork state)

Creep period	N _{pm} ⁽⁰⁾		M _{pm} ⁽⁰⁾	
	tB [kN]	tE [kN]	tB [kNm]	tE [kNm]
Storage	-1956.7	-1763.7	-931.47	-864.86
Utilization	-1763.7	-1327.8	-864.86	-779.14

tA=Begin, tE=End creep period

Prestress steel relaxation		
Lay. No.	Storage $\Delta\sigma_{p,r1}$ [N/mm ²]	Utilization $\Delta\sigma_{p,r2}$ [N/mm ²]
1	-0.09	-10.88
2	-0.09	-10.92
3	-0.09	-10.97
4	-0.10	-11.01
5	-0.10	-11.06
6	-0.10	-11.11
7	-0.10	-11.15
8	-0.10	-11.20



Prestr. steel, losses due to creeping, shrinking and relaxation:		
Lay. No.	Storage $\Delta\sigma_{p,csr1}^{(0)}$ [N/mm ²]	Utilization $\Delta\sigma_{p,csr2}^{(0)}$ [N/mm ²]
1	-67.25	-114.61
2	-65.72	-115.19
3	-64.19	-115.77
4	-62.66	-116.36
5	-61.13	-116.94
6	-59.60	-117.52
7	-58.07	-118.11
8	-56.54	-118.69

Stress in rebars due to creeping,shrinking and relaxation:		
Lay. No.	Storage $\Delta\sigma_{s,csr1}^{(0)}$ [N/mm ²]	Utilization $\Delta\sigma_{s,csr2}^{(0)}$ [N/mm ²]
1	-70.93	-107.90
2	-31.67	-121.91
3	-27.04	-123.56

Bending with Normal Force ULS

L.	Creep period	Cross-section	Tens-zone	z [cm]	M _{Rd} [kNm]	M _{Ed} [kNm]	η (>1.0)	
1	tB Storage	P	top	82.3	426.83	MEd < 0	n/a	#1
2	tE Storage	P	bottom	87.4	2610.30	543.37	4.80	
3	tB Storage/Erection	P	top	82.3	426.83	64.26	6.64	#1
4	tE Storage/Erection	P	bottom	87.4	2610.30	MEd < 0	n/a	
5	tE Utilization	P	top	89.0	588.56	MEd < 0	n/a	
6	tE Utilization	P	bottom	86.9	2637.16	1471.73	1.79	

#1: fck(t) = 0.73 * fck

Interim results : Ultimate elongation and internal forces

L.	ε _c [‰]	ε _s [‰]	x [cm]	Ap [cm ²]	As [cm ²]	Zp [kN]	Zs [kN]	Dc [kN]	Dp [kN]	Ds [kN]
1	3.500	3.100	58.2	0.0	12.6	0.0	546.9	1848.1	-1436.5	166.9
2	3.500	16.300	19.4	20.5	4.0	2871.2	178.9	2643.2	0.0	366.7
3	3.500	3.100	58.2	0.0	12.6	0.0	546.9	1848.1	-1436.5	166.9
4	3.500	16.300	19.4	20.5	4.0	2871.2	178.9	2643.2	0.0	366.7
5	3.500	6.700	37.7	0.0	12.6	0.0	549.4	1641.4	-1223.8	164.0
6	3.500	16.300	19.4	20.5	4.0	2862.7	178.7	2643.2	0.0	451.2

Shear Resistance

Design value shear force						
L.	Creep period	Combination	V _{Ed,0} [kN]	M _{Ed} [kNm]	dV [kN]	due to
1	tB Storage	QMax	133.8	543.35	-30.8	Vccd
2	tE Storage	QMax	133.8	543.35	-30.8	Vccd
3	tB Storage/Erection	QMax	134.5	-64.26	0.0	-----
4	tE Storage/Erection	QMax	134.5	-64.26	0.0	-----
5	tB Utilization	QMax	356.2	1471.72	-83.8	Vccd
6	tE Utilization	QMax	356.2	1471.72	-83.8	Vccd



Effective cross-section									
L.	Cross-section	Tens-zone	b _w [cm]	d [cm]	z [cm]	A _c [cm ²]	A _{sl} [cm ²]	σ _{cp} [N/mm ²]	V _{Rdc} [kN]
1	P	bottom	19.0	110.0	87.4	2940.8	24.5	4.86	277.2
2	P	bottom	19.0	110.0	87.4	2940.8	24.5	5.40	308.1
3	P	top	19.0	104.2	82.3	2940.8	12.6	4.86	241.5
4	P	top	19.0	104.2	82.3	2940.8	12.6	5.40	268.4
5	P	bottom	19.0	110.0	86.9	2940.8	24.5	5.40	308.1
6	P	bottom	19.0	110.0	86.9	2940.8	24.5	4.06	266.3

Shear design v ₁ = 0.480									
L.	V _{Ed} [kN]	V _{Ed,red} [kN]	a _{cw}	cotθ	a _{sw} [cm ² /m]	Note	a _l [cm]	V _{Rd,max} [kN]	
1	103.0	103.0	1.247	1.477	1.83	Min	64.6	1196.6	#1
2	103.0	103.0	1.162	1.261	2.15	Min	55.1	1503.5	
3	134.5	134.5	1.247	2.048	1.83	Min	84.3	956.9	#1
4	134.5	134.5	1.162	1.748	2.15	Min	72.0	1253.3	
5	272.4	272.4	1.162	3.353	2.15	Min	145.7	840.8	
6	272.4	272.4	1.122	2.500	2.88	Var	108.6	1022.2	

#1: f_{ck}(t) = 0.73 * f_{ck}

Check of crack width limit in SLS

perm. crack width: w_k < 0 mm, Frequent load combination

L.	Creep period	Cross-section	Tens-zone	r _{sub} r _{inf}	max.σ _s [N/mm ²]	S _{r,max} [mm]	ε _{sm} -ε _{cm} [‰]	w _k [mm]
1	tB Storage	P	top	1.00	CS completely compressed			
2	tE Storage	P	bottom	1.00	CS completely compressed			
3	tB Storage/Erection	P	top	1.00	87.39	578	0.262	0
4	tE Storage/Erection	P	bottom	1.00	CS completely compressed			
5	tE Utilization	P	top	1.00	CS completely compressed			
6	tE Utilization	P	bottom	1.00	CS completely compressed			

Internal forces and elongation								
L.	N _{aes} [kN]	M _{aes} [kNm]	max.σ [N/mm ²]	State I XOI [cm]	Φ _{eff}	ε _c [‰]	State II XOII [cm]	
1	-1956.7	-529.00	-0.32	116.0	0.00	-0.738	68.9	
2	-1763.7	-462.38	-13.56	117.5				
3	-1956.7	-979.07	4.78	94.0				
4	-1763.7	-912.46	-21.22	93.2				
5	-1327.8	136.55	-5.83	171.0				
6	-1327.8	177.42	-1.26	142.0				

XOI: Pressure zone height in state I XOII: Pressure zone height in state II

L.	h _{c,ef} [cm]	A _{ceff} [cm ²]	ξ ₁	A _p [cm ²]	A _s [cm ²]	ρ _{p,ef} [%]	ρ _{tot} [%]	k1	k2	k3	c [cm]	k4
3	14.9	892.3	1.29	0.0	6.3	0.704	0.704	0.80	0.50	3.40	2.8	0.425

Internal forces cracking and strains (state II)								
L.	N _{aes} [kN]	M _{aes} [kNm]	max.σ [N/mm ²]	State I XOI [cm]	Φ _{eff}	ε _c [‰]	State II XOII [cm]	
3	-1763.7	-861.70	4.07	94.6				

XOI: Pressure zone height in state I XOII: Pressure zone height in state II



Minimum reinforcement for crack control:

L.	Creep period	Cross-section	Tens-zone	r_{sup} r_{inf}	σ_t [N/mm ²]	req. As [cm ²]	exist. As [cm ²]
1	tB Storage	P	top	1.00	0.30	< 4.07	not req.
2	tE Storage	P	bottom	1.00	-13.56	< 4.07	not req.
3	tB Storage/Erection	P	top	1.00	4.65	<= 0 cm ²	
4	tE Storage/Erection	P	bottom	1.00	-21.22	< 4.07	not req.
5	tE Utilization	P	top	1.00	-4.86	< 4.07	not req.
6	tE Utilization	P	bottom	1.00	1.77	< 4.07	not req.

					Web				Flange			
L.	D [mm]	x0IZ [cm]	A _p [cm ²]	ξ ₁	k	k _c	A _{ct} [cm ²]	A _s [cm ²]	k	k _c	A _{ct} [cm ²]	A _s [cm ²]
3	20	18.9	0.0	0.00	0.65	0.00	359.7	-nan(ind)	0.97	0.63	639.0	9.0
x0IZ: tensile zone in state I due to cracking forces												

Ductility reinforcement in precompressed tensile zone:

b [cm ³]	f _{ctm} [N/mm ²]	Z _s [cm]	req. As [cm ²]	exist. As [cm ²]
19	4.07	110.0	4.4	4.0

Stress checks SLS

Concrete edge stresses in state I due to prestress, creep, shrinkage and relaxation			
		$\sigma_{R, \text{Prestress}}$	
L.	due to	top [N/mm ²]	bottom [N/mm ²]
1	Prestr. release anchorage	4.24	-22.16
2	csr storage	-0.13	1.76
3	csr utilisation	0.43	2.86

Tab. Compr stresses of concrete					
		M_{Ed}		$\sigma_{c, \text{Prestress}}$	
L.	Creep period	Cross-section	+ = Max - = Min	Cc,Pk [N/mm ²]	Qc,Pk [N/mm ²]
1	tB Storage	P	--	-15.31	-15.31
2	tE Storage	P	--	-13.56	-13.56
3	tB Storage/Erection	P	--	-27.31*	
4	tE Storage/Erection	P	--	-22.83	
5	tB Utilization	P	+-	-8.74	-6.26
6	tE Utilization	P	+-	-8.31	-5.83

Tab. Steel- and Concrete tension stress						
		M_{Ed}		σ_o	σ_s	σ_t
L.	Creep period	Cross-section	+ = Max - = Min	Cc,Pm [N/mm ²]	Cc,Pk [N/mm ²]	Cc,Pk [N/mm ²]
1	tB Storage	P	+-	900.09	< 0	ZII
2	tE Storage	P	+-	849.73	< 0	ZII
3	tB Storage/Erection	P	---	899.12	87.39	ZII
4	tE Storage/Erection	P	---	820.77	84.70	ZII
5	tB Utilization	P	++	881.60	< 0	ZII
6	tE Utilization	P	+++	779.85	< 0	1.77

Pk= Prestress char. value, Pm= prestress mean value, Still: State II

Selected section x = 0.08 m from left support

Internal force combinations from external loading

LAC: dominant variable action (leading action)

ULS-PT : permanent + transient design situation (fundam. combination)

SLS-Cc : characteristic combination

SLS-Fc : frequent combination

SLS-Qc : quasi-permanent combination



maximum moment : [kNm]

	ULS-PT	SLS-Cc	SLS-Fc	SLS-Qc
Storage	13.29	9.83	9.83	9.83
Storage/Erection	-0.17	-0.17	-0.17	-0.17
Utilization	36.70	28.27	23.78	22.75
LAc	10	10	10	-

Minimum moment : [kNm]

	ULS-PT	SLS-Cc	SLS-Fc	SLS-Qc
Storage	9.80	9.83	9.83	9.83
Storage/Erection	-0.23	-0.17	-0.17	-0.17
Utilization	22.73	22.75	22.75	22.75
LAc	-	-	-	-

maximum shear force:[kN]

	ULS-PT
Storage	166.7
Storage/Erection	-2.0
Utilization	458.5
LAc	10

Effective Tendons (prestressed formwork state for t = t0 (sto))

	No.	Area	Distance	Prestress		tens.force		Shorttime
Layer No.		Ap [cm²]	f.bottom [cm]	max [N/mm²]	min [N/mm²]	max [kN]	min [kN]	Relaxation [N/mm²]
1	3	2.8	8.5	247.68	152.10	69.1	42.4	-0.05
2	3	2.8	12.3	247.68	152.10	69.1	42.4	-0.05
3	3	2.8	16.1	247.68	152.10	69.1	42.4	-0.05
4	3	2.8	19.9	247.68	152.10	69.1	42.4	-0.05
5	3	2.8	23.7	247.68	152.10	69.1	42.4	-0.05
6	3	2.8	27.5	247.68	152.10	69.1	42.4	-0.05
7	3	2.8	31.3	247.68	152.10	69.1	42.4	-0.05
8	1	0.9	35.1	247.68	152.10	23.0	14.1	-0.05

$\Delta\sigma(Tt0) = -39 \text{ N/mm}^2$ due to heat treatment

Untensioned reinforcement

Layer	Number	Diameter [mm]	Area [cm²]	LE [cm]
1	2	16	4.0	3.6
2	2	20	6.3	81.1
3	2	20	6.3	92.3

Cross-section Precast :

Layer of cross-section from top to bottom			
Nr	Width [cm]	Distance [cm]	Remarks
1	60.0	0.0	Web begin Web end
2	60.0	15.0	
3	19.0	23.2	
4	19.0	96.1	

Cross-section Values

	brutto			ideal		
	Ac [cm²]	zu [cm]	Ic [cm⁴]	Ai [cm²]	zi [cm]	Ii [cm⁴]
Precast cross-section	2609.7	59.6	2239971	2770.2	58.5	2496523



Internal forces from prestress (mean values, prestressed formwork state)

Creep period	$N_{pm}^{(0)}$		$M_{pm}^{(0)}$	
	tB [kN]	tE [kN]	tB [kNm]	tE [kNm]
Storage	-506.7	-240.7	-192.30	-101.51
Utilization	-391.9	-25.8	-165.30	-57.77

tA=Begin, tE=End creep period

Prestress steel relaxation		
Lay. No.	Storage $\Delta\sigma_{p,r1}$ [N/mm ²]	Utilization $\Delta\sigma_{p,r2}$ [N/mm ²]
1	-0.00	-0.50
2	-0.00	-0.51
3	-0.00	-0.52
4	-0.00	-0.53
5	-0.00	-0.53
6	-0.00	-0.54
7	-0.00	-0.55
8	-0.00	-0.55

Prestr. steel, losses due to creeping, shrinking and relaxation:		
Lay. No.	Storage $\Delta\sigma_{p,csr1}^{(0)}$ [N/mm ²]	Utilization $\Delta\sigma_{p,csr2}^{(0)}$ [N/mm ²]
1	-36.33	-102.24
2	-35.67	-101.24
3	-35.02	-100.25
4	-34.37	-99.25
5	-33.71	-98.26
6	-33.06	-97.26
7	-32.41	-96.27
8	-31.75	-95.27

Stress in rebars due to creeping,shrinking and relaxation:		
Lay. No.	Storage $\Delta\sigma_{s,csr1}^{(0)}$ [N/mm ²]	Utilization $\Delta\sigma_{s,csr2}^{(0)}$ [N/mm ²]
1	-38.12	-105.77
2	-24.44	-84.82
3	-22.46	-81.80

Bending with Normal Force ULS

L.	Creep period	Cross-section	Tens-zone	z [cm]	M_{Rd} [kNm]	M_{Ed} [kNm]	η (>1.0)	
1	tB Storage	P	top	66.6	504.73	$M_{Ed} < 0$	n/a	#1
2	tE Storage	P	bottom	69.0	2032.94	13.29	152.91	
3	tB Storage/Erection	P	top	66.6	504.73	0.23	2170.79	#1
4	tE Storage/Erection	P	bottom	69.0	2032.94	$M_{Ed} < 0$	n/a	
5	tB Utilization	P	top	60.7	542.47	$M_{Ed} < 0$	n/a	
6	tE Utilization	P	bottom	69.1	2017.85	36.70	54.98	

#1: $f_{ck}(t) = 0.73 \cdot f_{ck}$



Interim results : Ultimate elongation and internal forces										
L.	ϵ_c [%]	ϵ_s [%]	x [cm]	A _p [cm ²]	A _s [cm ²]	Z _p [kN]	Z _s [kN]	D _c [kN]	D _p [kN]	D _s [kN]
1	3.500	10.300	23.4	9.3	12.6	338.5	553.0	743.6	-35.3	166.8
2	3.500	13.500	19.1	20.5	4.0	2769.6	178.1	2597.6	0.0	355.4
3	3.500	10.300	23.4	9.3	12.6	338.5	553.0	743.6	-35.3	166.8
4	3.500	13.500	19.1	20.5	4.0	2769.6	178.1	2597.6	0.0	355.4
5	3.500	12.500	20.2	9.3	12.6	433.0	554.8	880.3	-56.0	163.7
6	3.500	14.300	18.2	20.5	4.0	2772.7	178.2	2492.6	0.0	399.4

Shear Resistance

Design value shear force							
L.	Creep period	Combination	V _{Ed,0} [kN]	M _{Ed} [kNm]	dV [kN]	due to	
1	tB Storage	QMax	166.7	13.27	-1.0	V _{ccd}	
2	tE Storage	QMax	166.7	13.27	-1.0	V _{ccd}	
3	tB Storage/Erection	QMax	-2.0	-0.23	0.0	-----	
4	tE Storage/Erection	QMax	-2.0	-0.23	0.0	-----	
5	tB Utilization	QMax	458.5	36.68	-2.6	V _{ccd}	
6	tE Utilization	QMax	458.5	36.68	-2.6	V _{ccd}	

Effective cross-section									
L.	Cross-section	Tens-zone	b _w [cm]	d [cm]	z [cm]	A _c [cm ²]	A _{sl} [cm ²]	σ _{cd} [N/mm ²]	V _{Rdc} [kN]
1	P	bottom	19.0	92.5	69.0	2609.7	24.5	1.75	160.5
2	P	bottom	19.0	92.5	69.0	2609.7	24.5	0.83	149.0
3	P	top	19.0	86.7	66.6	2609.7	12.6	1.75	131.9
4	P	top	19.0	86.7	66.6	2609.7	12.6	0.83	119.0
5	P	bottom	19.0	92.5	69.1	2609.7	24.5	1.35	162.8
6	P	bottom	19.0	92.5	69.1	2609.7	24.5	0.09	129.5

Shear design v1 = 0.480

Check V_{Rd,s} not requ., asw und cotθ from the last construction phase

L.	V _{Ed} [kN]	V _{Ed,red} [kN]	a _{cw}	cotθ	asw [cm ² /m]	Note	a _l [cm]	V _{Rd,max} [kN]	
1	165.8	165.8	1.072	2.500	2.21	Var	86.2	603.2	#1
2	165.8	165.8	1.025	2.500	2.21	Var	86.2	741.3	
3	2.0	2.0	1.072	1.000	1.83	Min	43.4	844.4	#1
4	2.0	2.0	1.025	1.000	2.15	Min	43.4	1037.7	
5	455.9	455.9	1.041	2.500	6.07	Var	86.4	753.7	
6	455.9	455.9	1.003	2.500	6.07	Var	86.4	726.3	

#1: f_{ck}(t) = 0.73 * f_{ck}

Check of crack width limit in SLS

perm. crack width: w_k < 0 mm, Frequent load combination

L.	Creep period	Cross-section	Tens-zone	r _{sup} r _{inf}	max. σ _s [N/mm ²]	S _{r,max} [mm]	ε _{sm} -ε _{cm} [%]	w _k [mm]
1	tB Storage	P	top	1.00	no cracks			
2	tE Storage	P	bottom	1.00	CS completely compressed			
3	tB Storage/Erection	P	top	1.00	no cracks			
4	tE Storage/Erection	P	bottom	1.00	CS completely compressed			
5	tB Utilization	P	top	1.00	no cracks			
6	tE Utilization	P	bottom	1.00	CS completely compressed			



Internal forces and elongation							
			State I		State II		
L.	N_{ges} [kN]	M_{ges} [kNm]	$\max.\sigma$ [N/mm ²]	X0I [cm]	φ_{eff}	ϵ_c [‰]	X0II [cm]
1	-506.7	-182.47	0.92	83.6			
2	-240.7	-91.68	-3.02	82.2			
3	-506.7	-192.47	1.07	82.3			
4	-240.7	-101.68	-3.25	79.9			
5	-391.9	-142.54	0.73	83.3			
6	-25.8	-33.99	-0.89	65.4			

X0I: Pressure zone height in state I X0II: Pressure zone height in state II

L.	$h_{c,ef}$ [cm]	A_{ceff} [cm ²]	ξ_1	A_p [cm ²]	A_s [cm ²]	$\rho_{p,ef}$ [%]	ρ_{tot} [%]	k1	k2	k3	c [cm]	k4
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Internal forces cracking and strains (state II)							
			State I		State II		
L.	N_{ges} [kN]	M_{ges} [kNm]	$\max.\sigma$ [N/mm ²]	X0I [cm]	φ_{eff}	ϵ_c [‰]	X0II [cm]

X0I: Pressure zone height in state I X0II: Pressure zone height in state II

Minimum reinforcement for crack control:

L.	Creep period	Cross-section	Tens-zone	r_{sub} r_{inf}	σ_t [N/mm ²]	req. A_s [cm ²]	exist. A_s [cm ²]
1	tB Storage	P	top	1.00	1.88	< 4.07	not req.
2	tE Storage	P	bottom	1.00	-3.02	< 4.07	not req.
3	tB Storage/Erection	P	top	1.00	2.03	< 4.07	not req.
4	tE Storage/Erection	P	bottom	1.00	-3.25	< 4.07	not req.
5	tB Utilization	P	top	1.00	2.05	< 4.07	not req.
6	tE Utilization	P	bottom	1.00	-0.78	< 4.07	not req.

					Web				Flange			
L.	D [mm]	x0IZ [cm]	A_o [cm ²]	ξ_1	k	k_c	A_{ct} [cm ²]	A_s [cm ²]	k	k_c	A_{ct} [cm ²]	A_s [cm ²]

x0IZ: tensile zone in state I due to cracking forces

Ductility reinforcement in precompressed tensile zone:

b [cm ³]	f_{ctm} [N/mm ²]	Zs [cm]	req. A_s [cm ²]	exist. A_s [cm ²]
19	4.07	92.5	3.7	4.0

Stress checks SLS

Concrete edge stresses in state I due to prestress, creep, shrinkage and relaxation			
L.	due to	top [N/mm ²]	bottom [N/mm ²]
1	Prestr. release anchorage	1.07	-6.34
2	csr storage	0.01	1.05
3	csr utilisation	0.19	2.93

Tab. Compr stresses of concrete						
L.	Creep period	Cross-section	M_{Ed} + = Max - = Min	$\sigma_{c,Pre}$ Cc,Pk [N/mm ²]	$\sigma_{c,Pre}$ Qc,Pk [N/mm ²]	
1	tB Storage	P	--	-6.11	-6.11	
2	tE Storage	P	--	-5.06	-5.06	
3	tB Storage/Erection	P	--	-6.34		
4	tE Storage/Erection	P	--	-5.29		
5	tB Utilization	P	--	-4.76	-4.76	
6	tE Utilization	P	--	-1.82	-1.82	



Tab. Steel- and Concrete tension stress						
L.	Creep period	Cross-section	M_{Ed} + = Max - = Min	σ_b Cc,Pm [N/mm ²]	σ_s Cc,Pk [N/mm ²]	σ_t Cc,Pk [N/mm ²]
1	tB Storage	P	---	229.01	3.47	0.92
2	tE Storage	P	+-	105.20	< 0	0.93
3	tB Storage/Erection	P	---	228.51	4.20	1.07
4	tE Storage/Erection	P	+-	104.70	< 0	1.08
5	tB Utilization	P	++	201.69	< 0	0.73
6	tE Utilization	P	++	21.02	< 0	0.92

Pk= Prestres char. value, Pm= prestress mean value, Still: State II

Lateral buckling (Stiglat)

Safety in installed state $\eta = 1.69 < 2.00$

Design buckling moment: $M_{kipp} = 4657.51$ kNm

existing moment : $M_{Ed} = 2763.72$ kNm without prestress

Combination of characteristic values

Interim values acc. to 'Beton- und Stahlbetonbau' 1985, H. 9,10,11

$E_{cm} = 37000$ N/mm ²	$G_{cm} = 14800$ N/mm ²	It, ly averaged
$I_t = 208188$ cm ⁴	$I_y = 394505$ cm ⁴	acc.to Rafla
$I_x = 11379011$ cm ⁴	$A_k = 4664.5$ MN ² cm ⁴	(It 60% as C.II)
$h_c = 1.58$ m	$\beta_1 = 0.000$	$\beta_2 = 0.003$
$k_1 = 3.540$	$k_2 = 1.000$	$k_3 = 0.920$
$M_k = 7415.48$ kNm	$W_{x0} = 123859$ cm ³	$x = 20.20$ m
$\sigma_B = 52.87$ N/mm ²	$\sigma_T = 33.21$ N/mm ²	$\lambda_V = 83.1$

(σ_T acc. eq.62calculated !)

a potentially nessecary reinforcement for torsion is not determined in the program

Lateral buckling check in erection state (acc. to Stiglat)

Height of left attachment point about LE beam

left Hmh = 114.0 cm right Hmh = 114.0 cm

Erection with lifting beam

Lateral buckling safety $\eta = 4.29 > 2.50$

Design buckling moment: $M_{kipp} = 2343.70$ kNm

existing moment : $M_{Ed} = 546.28$ kNm without prestress

Interim values acc. to 'Beton- und Stahlbetonbau' 1985, H. 9,10,11

$\beta_4 = 0.000$	$\delta = 0.000$	$\gamma = 1.000$
$f = 0.331$ m	$A_k = 4664.5$ MN ² cm ⁴	$p = 0.752$
$j(a) = 0.095$	$a = 1.478$	$q_{kl} = 47.76$ kN/m
$W_{x0} = 148769$ cm ³	$M_k = 2700.05$ kNm	$x = 16.83$ m
$\sigma_B = 18.15$ N/mm ²	$\sigma_T = 15.75$ N/mm ²	$\lambda_V = 141.8$

Anchorage by bond (over the left bearing)

$l_{pt2} = 1.20$ m Distance first bending crack $l_r = 3.37$ m
 $\eta_{p2} = 1.20$ $f_{bpd} = 2.28$ N/mm²

x [m]	Z_p [kN]	Z_s [kN]	T_{Ed} [kN]	$\eta = (Z_p + Z_s)/T_{Ed}$	Util
0.15	395.3	178.1	664.5	0.86	1.16
0.20	523.2	178.1	691.7	1.01	0.99
0.40	1046.5	178.0	799.3	1.53	0.65
0.60	1569.7	178.0	901.1	1.94	0.52
0.80	2093.0	178.0	1007.5	2.25	0.44
1.00	2616.2	178.1	1101.6	2.54	0.39
1.20	2831.2	178.2	1185.0	2.54	0.39
1.40	2832.3	178.2	1268.4	2.37	0.42
1.60	2833.2	178.2	1351.7	2.23	0.45
1.80	2834.1	178.2	1435.1	2.10	0.48
2.00	2845.5	178.4	1518.5	1.99	0.50



x [m]	Z_p [kN]	Z_s [kN]	T_{Ed} [kN]	$\eta = (Z_p + Z_s) / T_{Ed}$	Util						
Z_p : resisting tensile force by the prestressed steel Z_s : resisting tensile force by the rebars T_{Ed} : tensile force to be anchored											
No. Lay.	Dist.LE [cm]	XA [m]	σ_p [N/mm ²]	Eq.	l_{bod} [m]	xk [m]	ΣZ_p [kN]	ΣZ_s [kN]	T_{Ed} [kN]	add. As [cm ²]	
1	8.5	0.00	619.00	8.21	2.15		Anchorage range uncracked				(PT)
2	12.3	0.00	629.03	8.21	2.14		Anchorage range uncracked				(PT)
3	16.1	0.00	639.06	8.21	2.13		Anchorage range uncracked				(PT)
4	19.9	0.00	649.09	8.21	2.12		Anchorage range uncracked				(PT)
5	23.7	0.00	659.11	8.21	2.11		Anchorage range uncracked				(PT)
6	27.5	0.00	669.13	8.21	2.10		Anchorage range uncracked				(PT)
7	31.3	0.00	679.15	8.21	2.34		Anchorage range uncracked				(PT)
8	35.1	0.00	689.17	8.21	2.33		Anchorage range uncracked				(PT)
XA: Beginning of the anchoring area of the steel layer (dist. from the corresp. binder side) Eq. 8.21.1: Anchorage area uncracked,σ _p acc.to fig. 8.17DE (b) Eq. 8.21.1: Anchorage area cracked,σ _p acc.to fig. 8.17DE (b) xk: decisive section in the anchoring area of the layer (distance from the beginning of the binder) add. As: Additional sagging reinforcement required for anchorage											

Anchorage by bond (over the right bearing)

$$l_{p12} = 1.20 \text{ m} \quad \text{Distance first bending crack} \quad l_r = 3.37 \text{ m}$$

$$\eta_{p2} = 1.20 \quad f_{bpd} = 2.28 \text{ N/mm}^2$$

x [m]	Z_p [kN]	Z_s [kN]	T_{Ed} [kN]	$\eta = (Z_p + Z_s) / T_{Ed}$	Util
28.30	2845.5	178.4	1518.5	1.99	0.50
28.50	2834.1	178.2	1435.1	2.10	0.48
28.70	2833.2	178.2	1351.7	2.23	0.45
28.90	2832.3	178.2	1268.4	2.37	0.42
29.10	2831.2	178.2	1185.0	2.54	0.39
29.30	2616.2	178.1	1101.6	2.54	0.39
29.50	2093.0	178.0	1007.5	2.25	0.44
29.70	1569.7	178.0	901.1	1.94	0.52
29.90	1046.5	178.0	799.3	1.53	0.65
30.10	523.2	178.1	691.7	1.01	0.99
30.15	395.3	178.1	664.5	0.86	1.16
Z_p : resisting tensile force by the prestressed steel Z_s : resisting tensile force by the rebars T_{Ed} : tensile force to be anchored					

No. Lay.	Dist.LE [cm]	XA [m]	σ_p [N/mm ²]	Eq.	l_{bod} [m]	xk [m]	ΣZ_p [kN]	ΣZ_s [kN]	T_{Ed} [kN]	add. As [cm ²]	
1	8.5	0.00	619.00	8.21	2.15		Anchorage range uncracked				(PT)
2	12.3	0.00	629.03	8.21	2.14		Anchorage range uncracked				(PT)
3	16.1	0.00	639.06	8.21	2.13		Anchorage range uncracked				(PT)
4	19.9	0.00	649.09	8.21	2.12		Anchorage range uncracked				(PT)
5	23.7	0.00	659.11	8.21	2.11		Anchorage range uncracked				(PT)
6	27.5	0.00	669.13	8.21	2.10		Anchorage range uncracked				(PT)
7	31.3	0.00	679.15	8.21	2.34		Anchorage range uncracked				(PT)
8	35.1	0.00	689.17	8.21	2.33		Anchorage range uncracked				(PT)
XA: Beginning of the anchoring area of the steel layer (dist. from the corresp. binder side) Eq. 8.21.1: Anchorage area uncracked, σ_p acc.to fig. 8.17DE (b) Eq. 8.21.1: Anchorage area cracked, σ_p acc.to fig. 8.17DE (b) xk: decisive section in the anchoring area of the layer (distance from the beginning of the binder) add. As: Additional sagging reinforcement required for anchorage											



Bursting Reinforcement at beginning of beam

$$y_{p,unfav} = 1.20 \quad l_{disp} = 1.35 \text{ m}$$

Initiation zone			Section over the last effective position of tension. member					
No.	from [m]	to [m]	Dist.LE [cm]	N_c [kN]	N_p [kN]	T_p [kN]	Factor Interpolation	req. As [cm ²]
1	0.00	1.35	36.1	-1286.3	1762.0	475.8	0.406	5.3

The bursting reinforcement must be arranged in zone of reduced dispersion length.
red. dispersion length indented wire w.o. strand $3/4 \cdot l_{disp} = 1.02 \text{ m}$

Bursting Reinforcement at end of beam

$$y_{p,unfav} = 1.20 \quad l_{disp} = 1.35 \text{ m}$$

Initiation zone			Section over the last effective position of tension. member					
No.	from [m]	to [m]	Dist.LE [cm]	N_c [kN]	N_p [kN]	T_p [kN]	Factor Interpolation	req. As [cm ²]
1	30.30	28.95	36.1	-1286.3	1762.0	475.8	0.406	5.3

The bursting reinforcement must be arranged in zone of reduced dispersion length.
red. dispersion length indented wire w.o. strand $3/4 \cdot l_{disp} = 1.02 \text{ m}$